

Statistical Modeling: Applications

Intermediate Social Statistics
Week 7 & 8 (1 & 8 March 2016)
Andy Eggers

Ordinal probit application: Hainmueller and Hiscox 2010

Two economic explanations for (variation in) anti-immigrant sentiment:

- **Labor market competition** → natives should oppose immigrants with skill levels similar to their own
- **Fiscal burden** → rich natives should be more opposed to low-skilled immigrants than poor natives (especially where immigrants use a lot of public services)



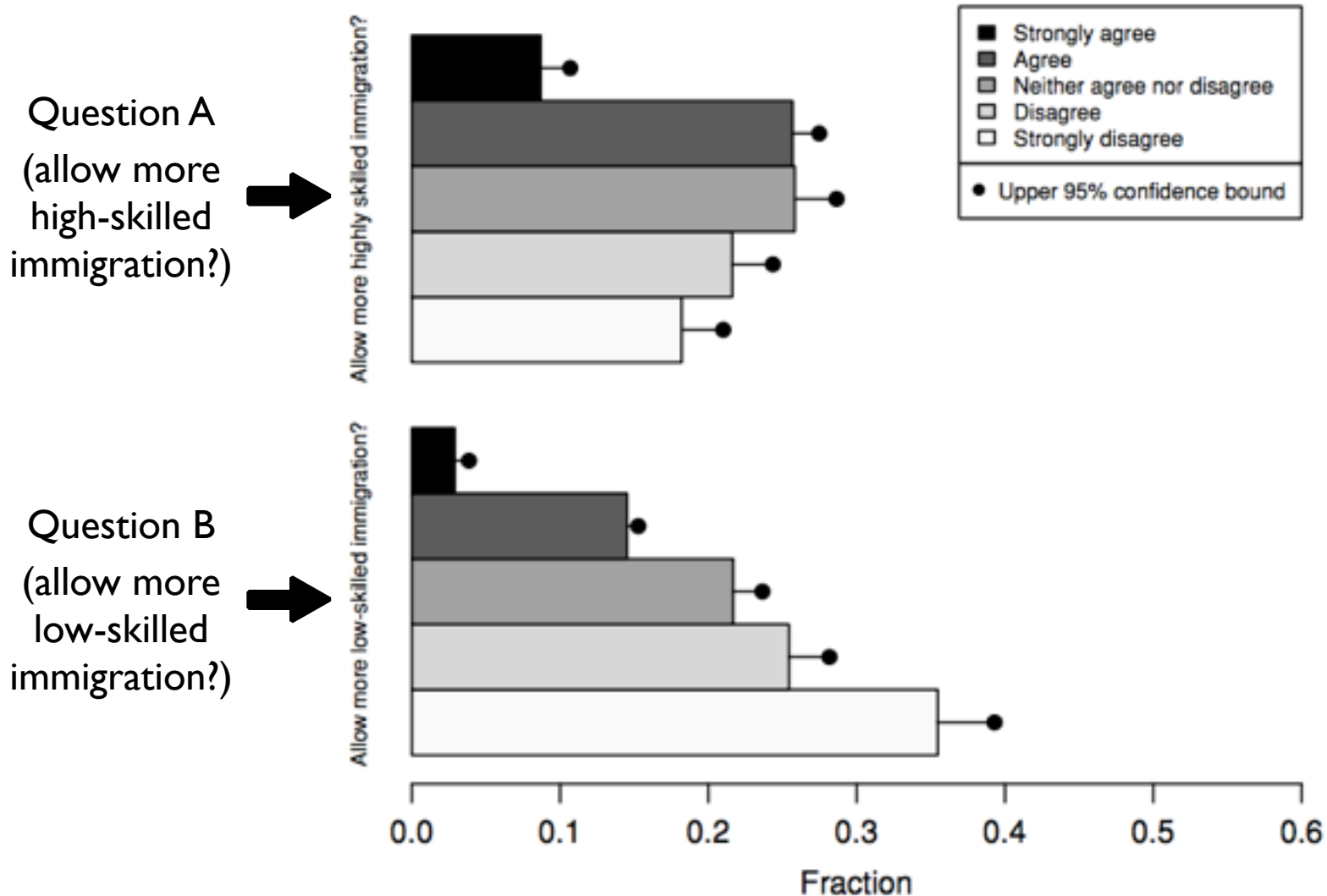
Hainmueller and Hiscox ask a sample of US respondents either

- A. Do you agree or disagree that the US should allow more **highly skilled immigrants** from other countries to come and live here?
- B. Do you agree or disagree that the US should allow more **low-skilled immigrants** from other countries to come and live here?

(Random whether respondent gets A or B)

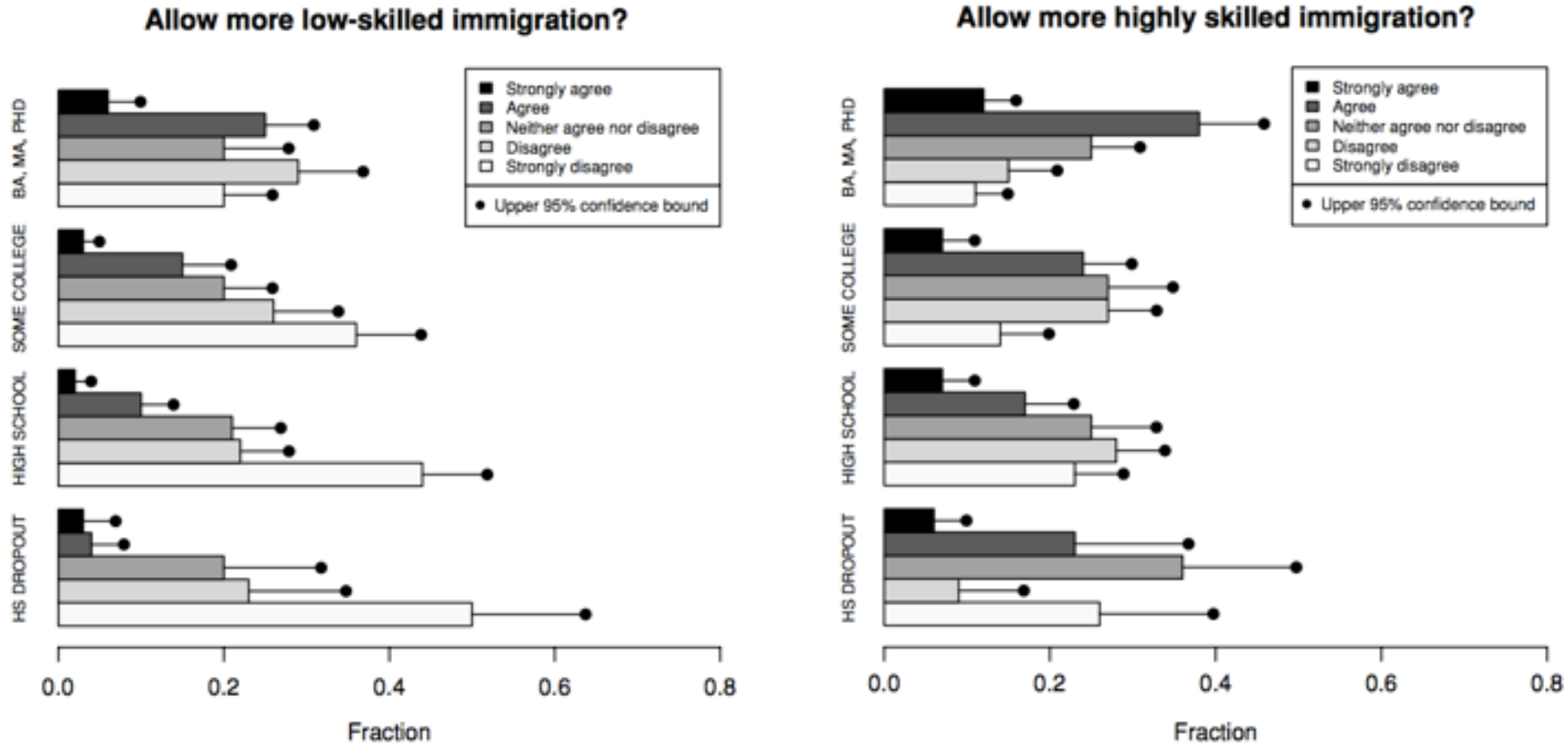
Hainmueller and Hiscox (2010)

FIGURE 2. Support for Highly Skilled and Low-skilled Immigration



Hainmueller and Hiscox (2010)

FIGURE 3. Support for Highly Skilled and Low-skilled Immigration by Respondents' Skill Level



Ordered probit

Motivations:

- **Predict** ordered outcome Y
- Characterize the determinants of a **latent variable** Y^* (e.g. support for immigration) underlying ordered outcome Y

1. Strongly disagree
2. Disagree
3. Neither agree nor disagree
4. Agree
5. Strongly agree

Ordered probit

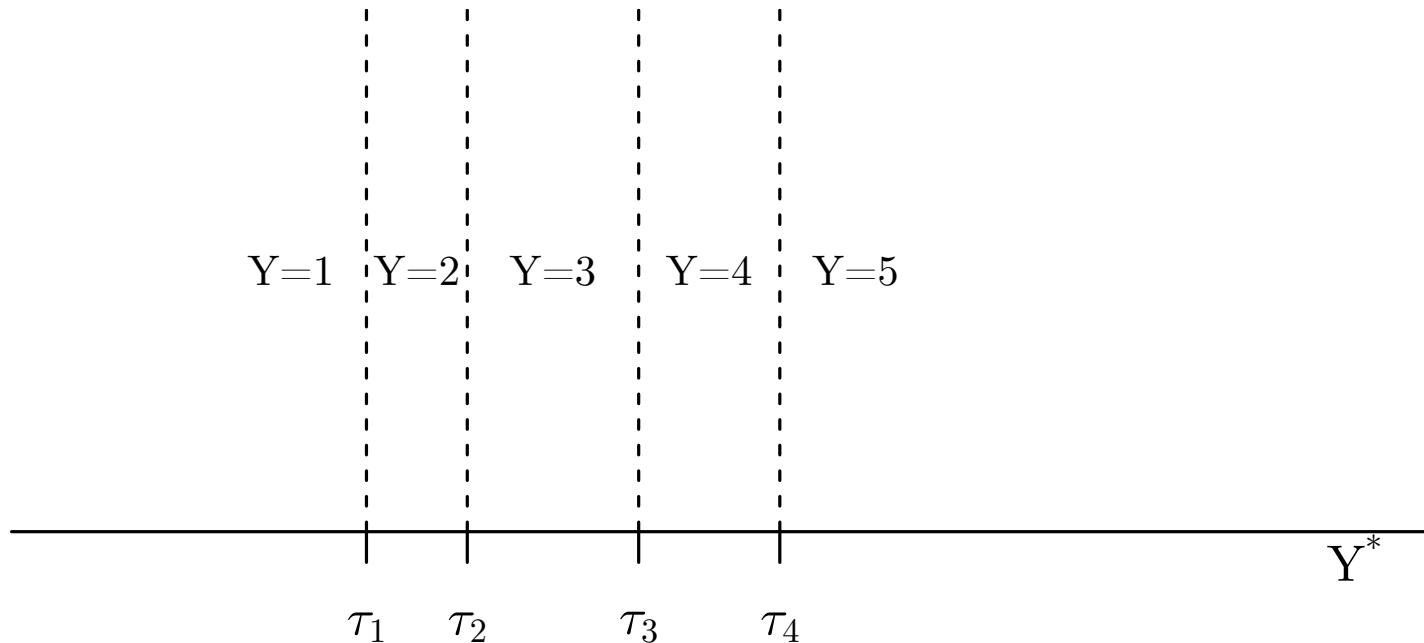
Suppose we observed Y^* (support for immigration), which perfectly predicts the response given:

$$Y = \begin{cases} 1, & \text{if } Y^* \leq \tau_1 \\ 2, & \text{if } Y^* \in (\tau_1, \tau_2] \\ 3, & \text{if } Y^* \in (\tau_2, \tau_3] \\ 4, & \text{if } Y^* \in (\tau_3, \tau_4] \\ 5, & \text{if } Y^* > \tau_4 \end{cases}$$

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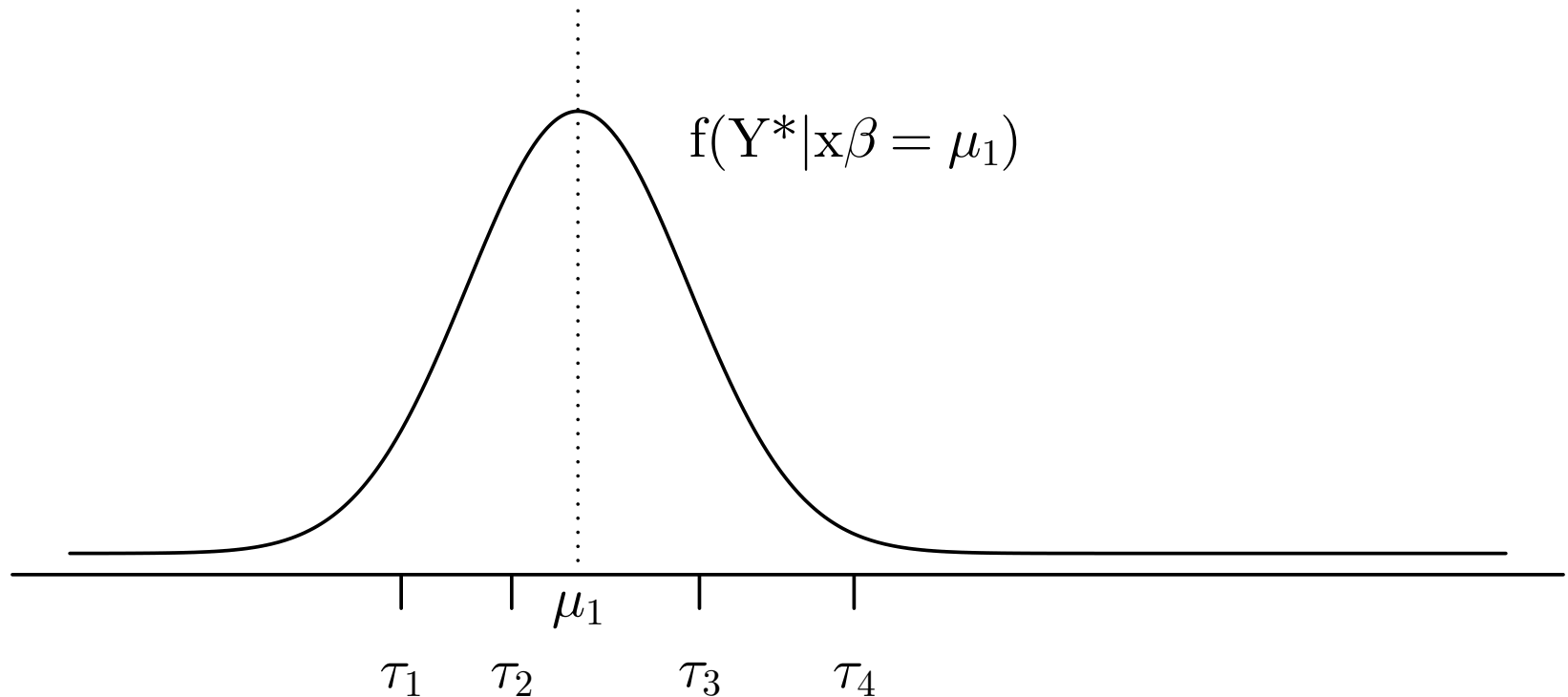
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Ordered probit

We don't observe Y^* , but we postulate that it is a linear function of covariates, plus error:

$$Y^* = x\beta + \epsilon$$
$$\epsilon \sim N(0, 1)$$

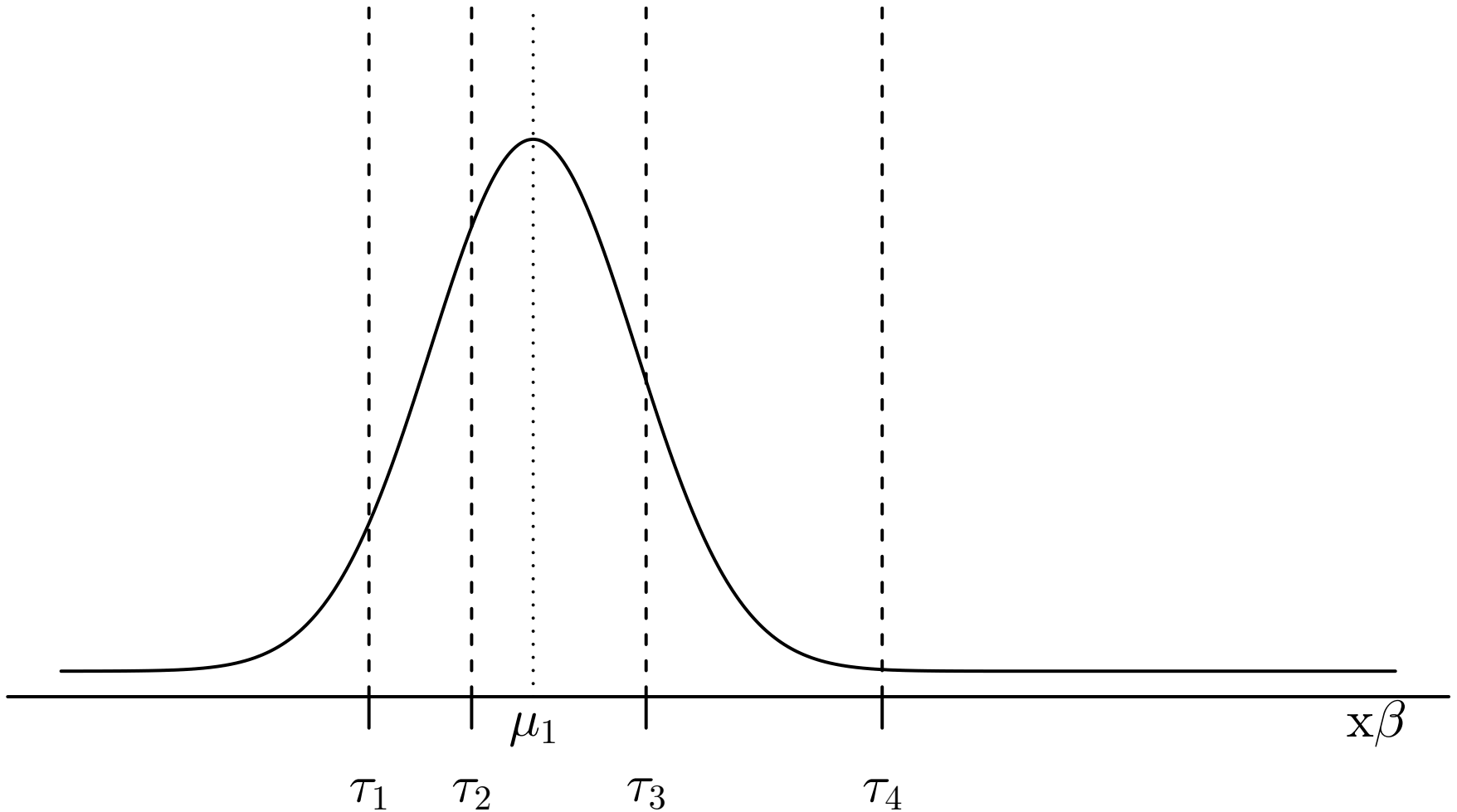


Ordered probit: visualization

That implies that given $\tau_1, \tau_2, \tau_3, \tau_4$ and $\mu_i = x_i\beta$ we know the probability of each outcome:

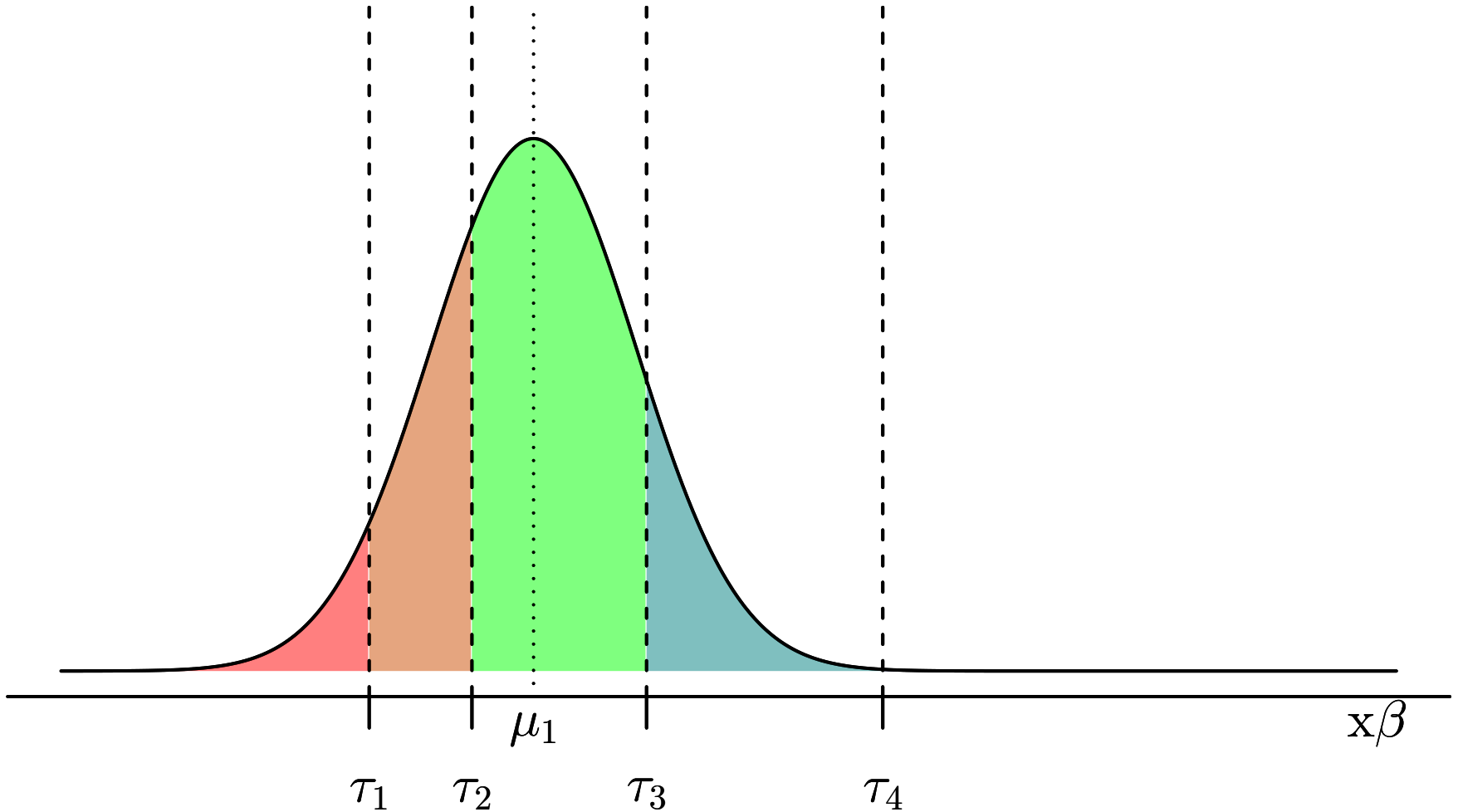
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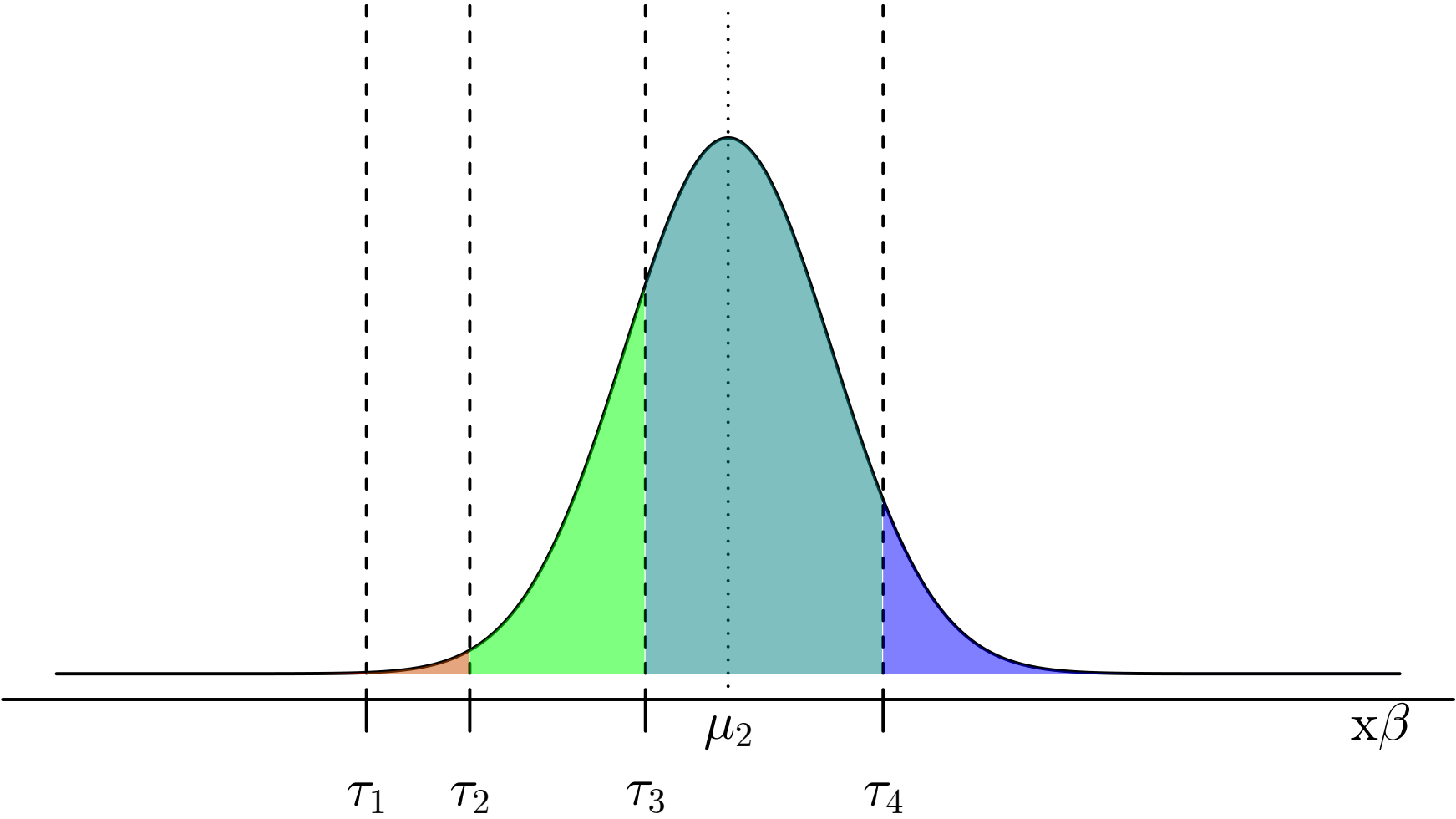


Ordered probit: visualization

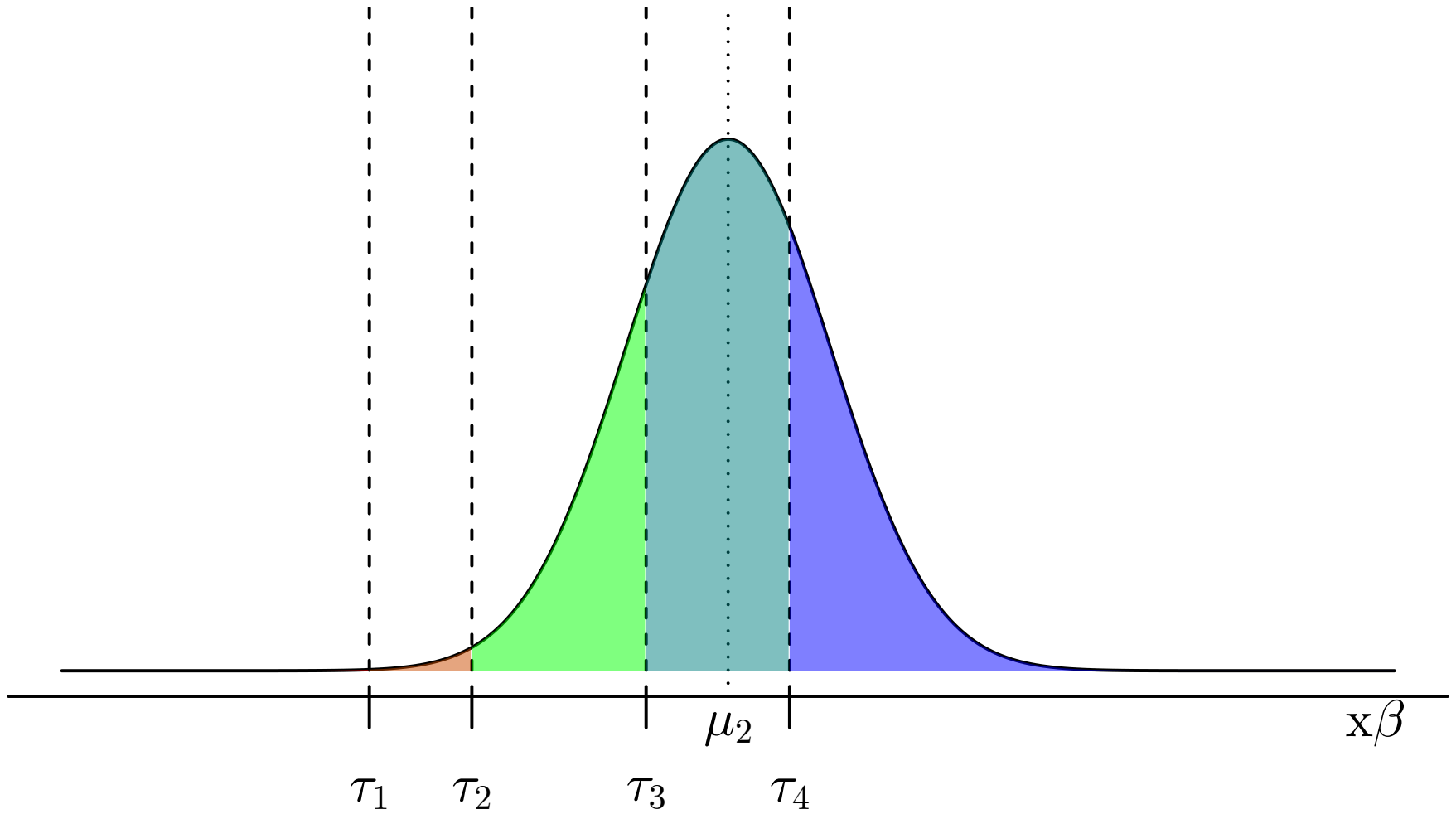
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Ordered probit: visualization (2)

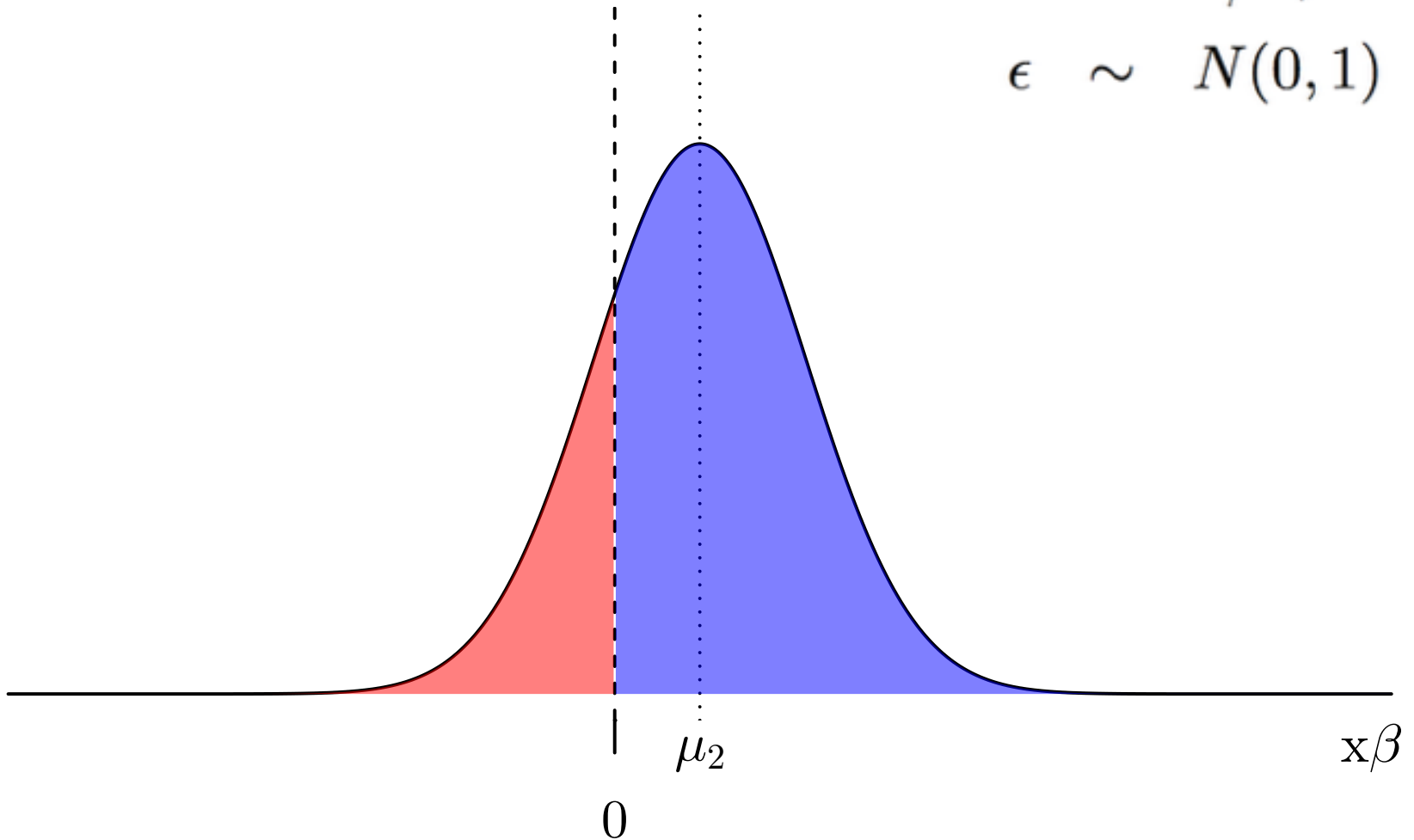


Ordered probit: visualization (3)



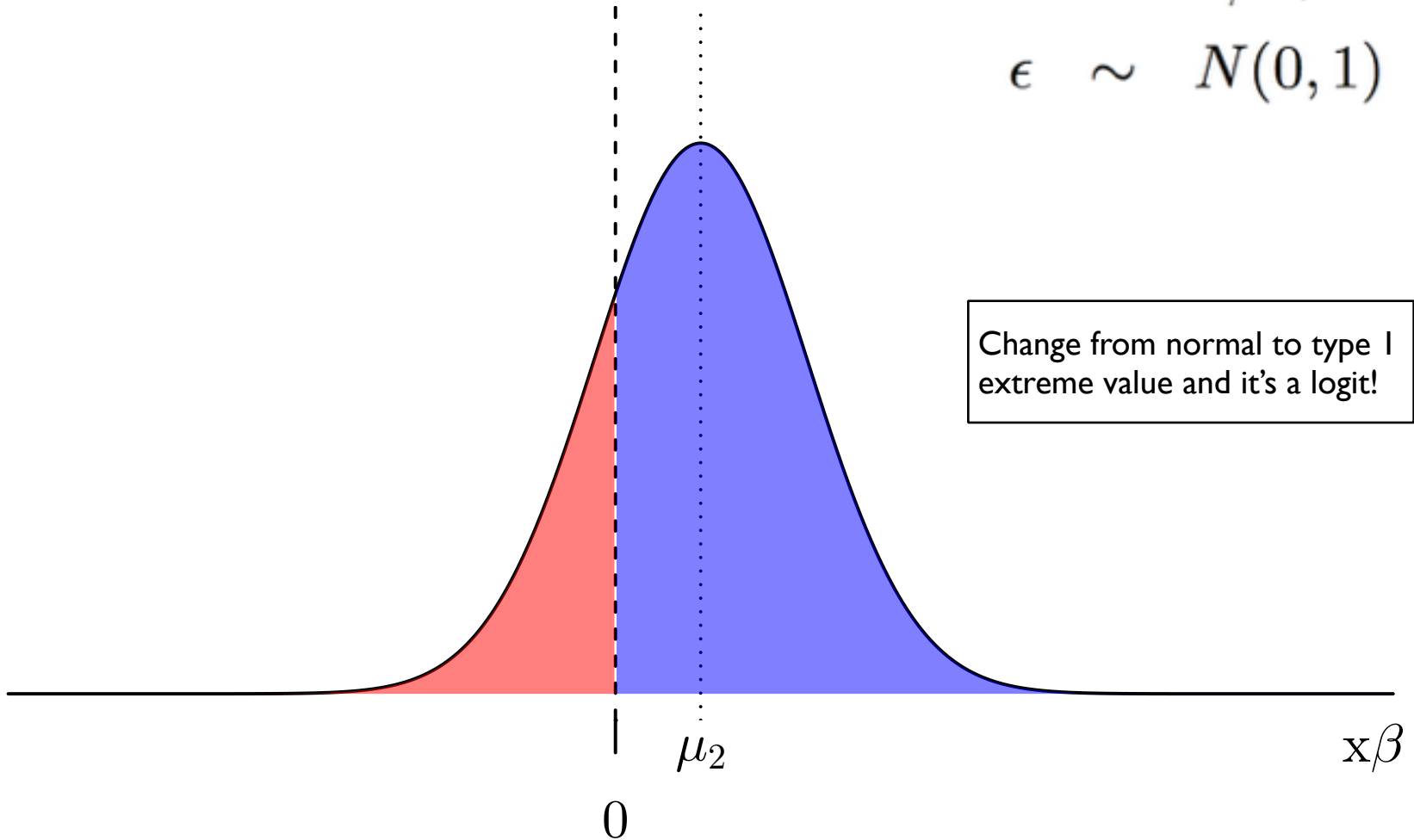
Binary probit: a special case with single threshold at 0

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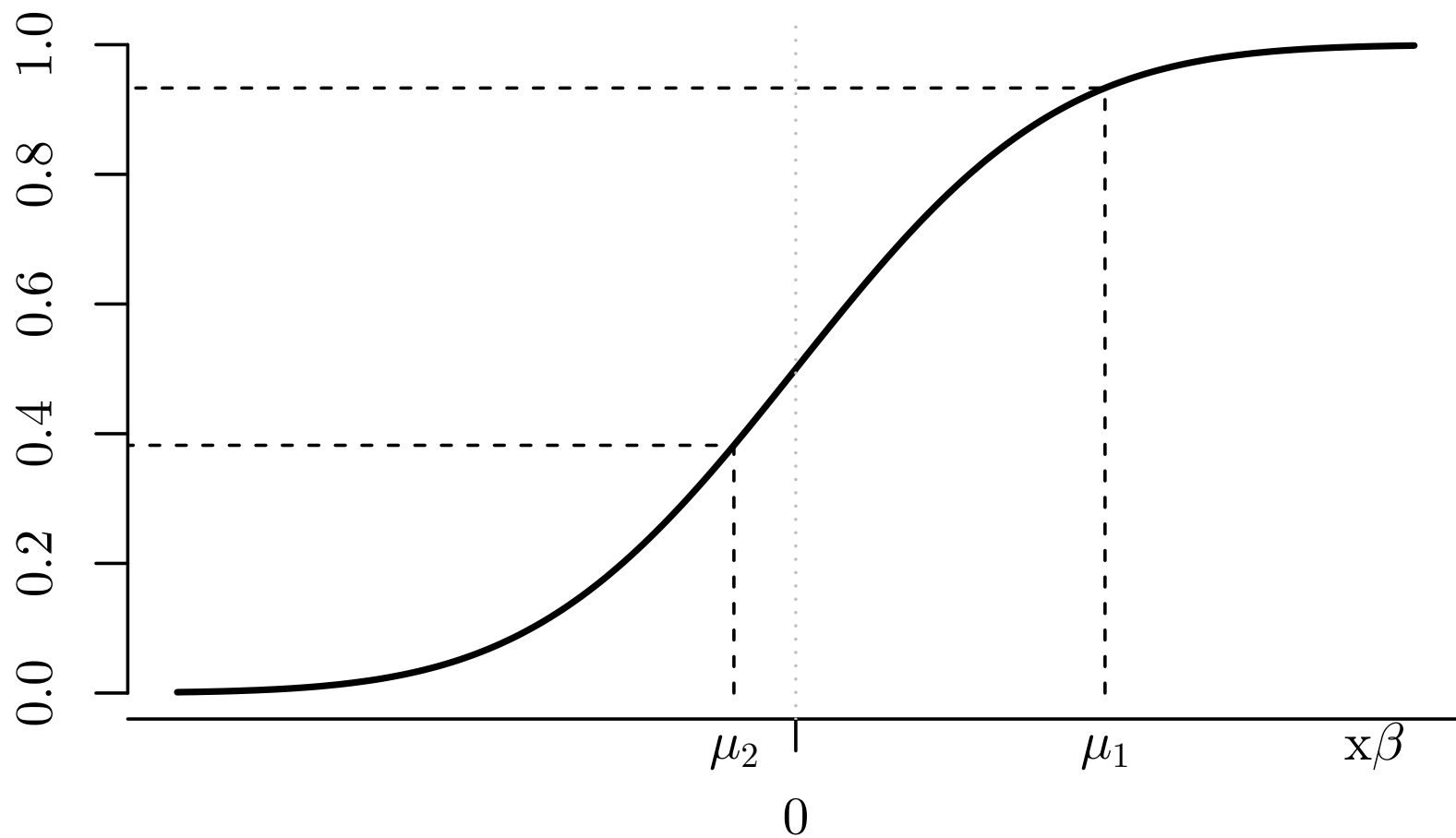


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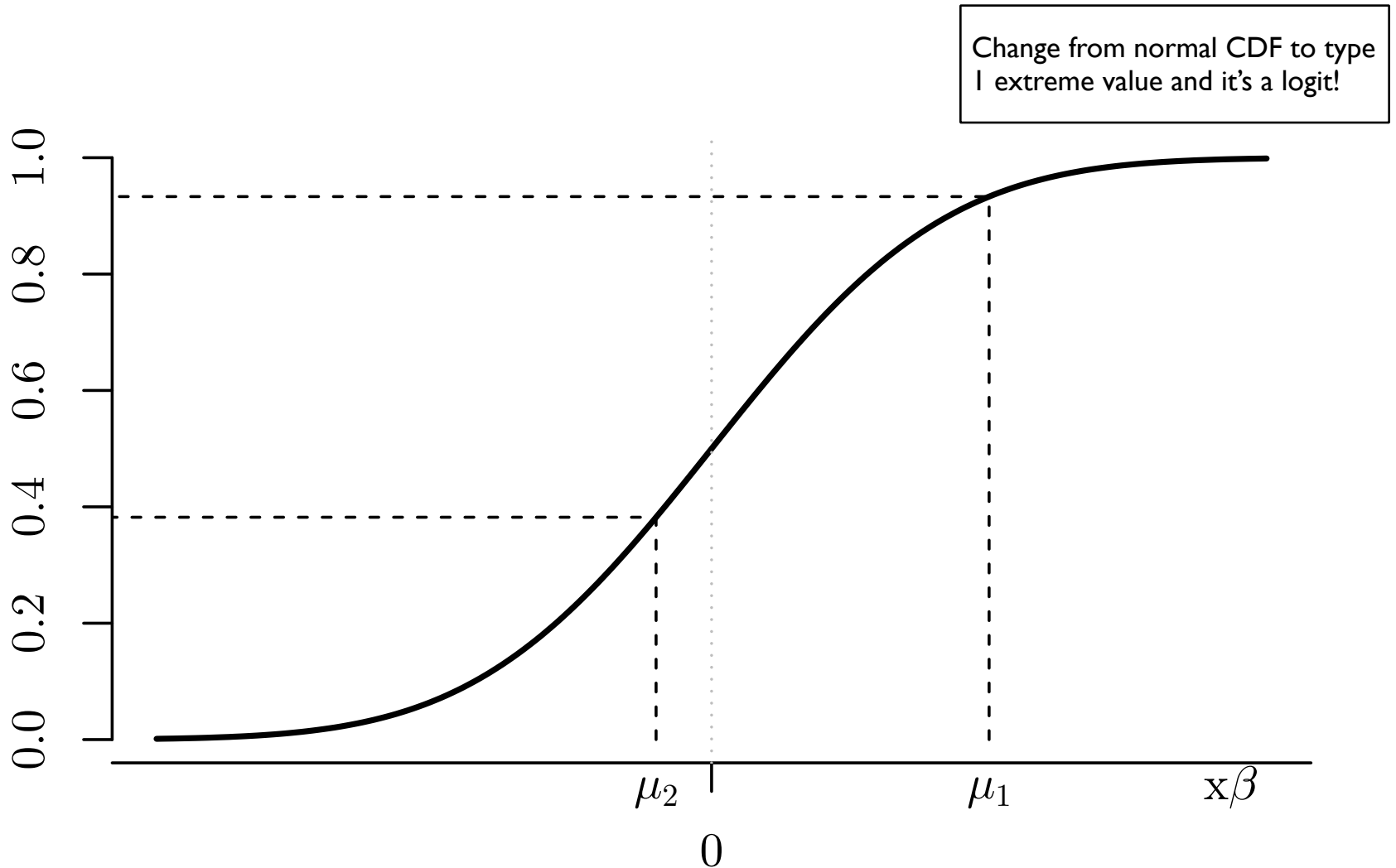
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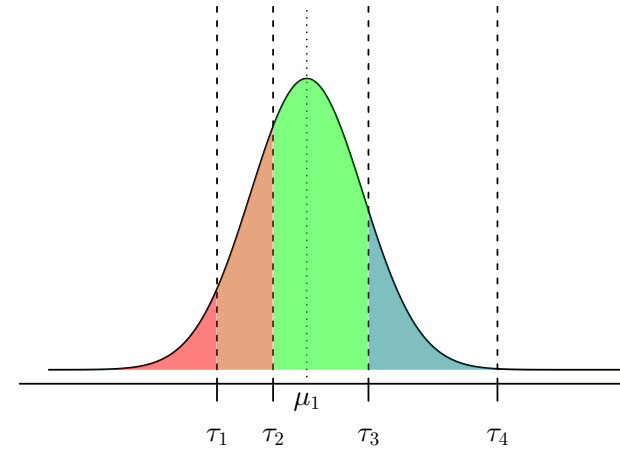


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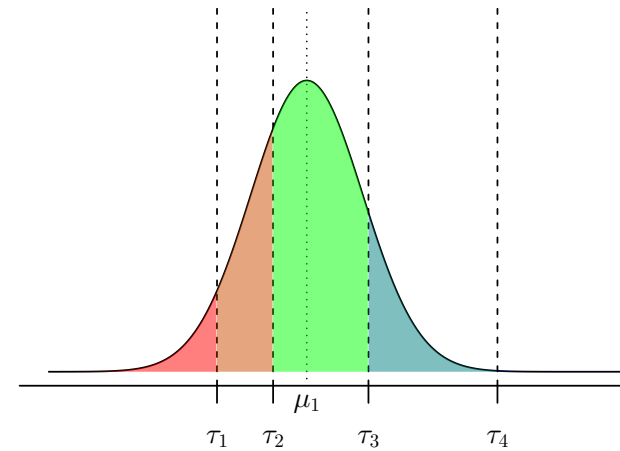
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What are the key assumptions of the standard ordered probit model? In what circumstances would these assumptions not hold? What might we miss?



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Some key points:

- model does not permit “polarization” of responses due to given X
 - if $X\beta$ implies outcome j , then increasing $X\beta$ makes outcomes below j less likely and outcomes above j more likely
 - (no different from OLS, other GLMs in that respect)
- standard model does not permit given X affecting probability of outcome 1 vs outcome 2 without affecting outcome 3, etc (but could imagine making cutoffs a function of covariates?)

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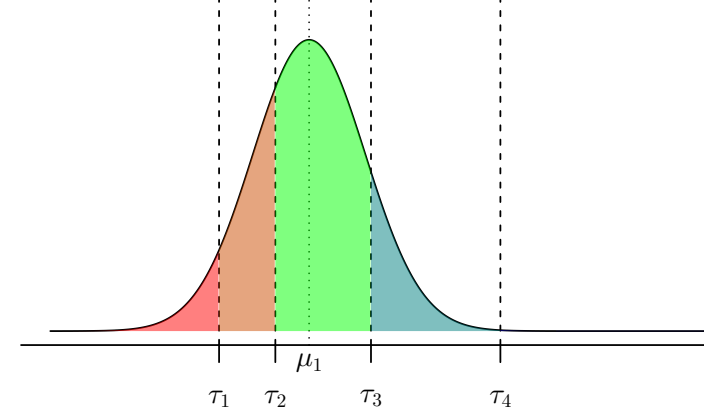
```
. oprobit sh_both hskframe ppeducat hskeduc xx* [pweight=weight1]
```

```
Iteration 0: log pseudolikelihood = -2418.2933
Iteration 1: log pseudolikelihood = -2306.2688
Iteration 2: log pseudolikelihood = -2306.1887
Iteration 3: log pseudolikelihood = -2306.1887
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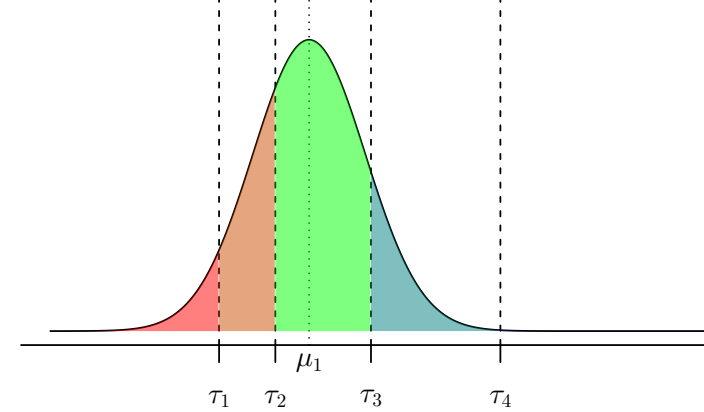
```
Ordered probit regression                Number of obs    =    1,589
                                         Wald chi2(8)     =    158.52
                                         Prob > chi2      =    0.0000
Log pseudolikelihood = -2306.1887       Pseudo R2       =    0.0464
```

sh_both	Coef.	Robust Std. Err.	z	P> z	[95% Conf. Interval]	
hskframe	.7261249	.2025688	3.58	0.000	.3290974	1.123152
ppeducat	.2683796	.0484328	5.54	0.000	.1734531	.3633061
hskeduc	-.0653202	.0667142	-0.98	0.328	-.1960777	.0654373
xxfemale	-.1771998	.0644352	-2.75	0.006	-.3034904	-.0509092
xxppagecat	-.0110243	.0196088	-0.56	0.574	-.0494569	.0274083
xxWhite	-.374742	.0990717	-3.78	0.000	-.5689189	-.1805651
xxBlack	-.4720909	.1352577	-3.49	0.000	-.7371911	-.2069907
xxHispanic	.0627729	.2058409	0.30	0.760	-.3406679	.4662136
/cut1	-.114744	.1910944			-.4892822	.2597941
/cut2	.5613041	.1905945			.1877457	.9348625
/cut3	1.254911	.1907666			.8810152	1.628807
/cut4	2.258038	.2003352			1.865388	2.650688

Ordered probit: estimation

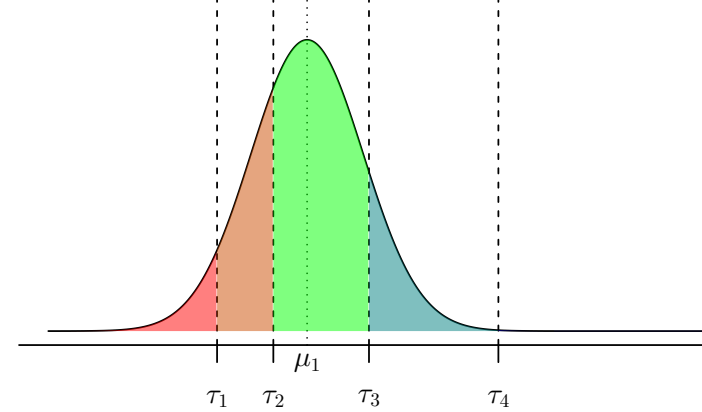


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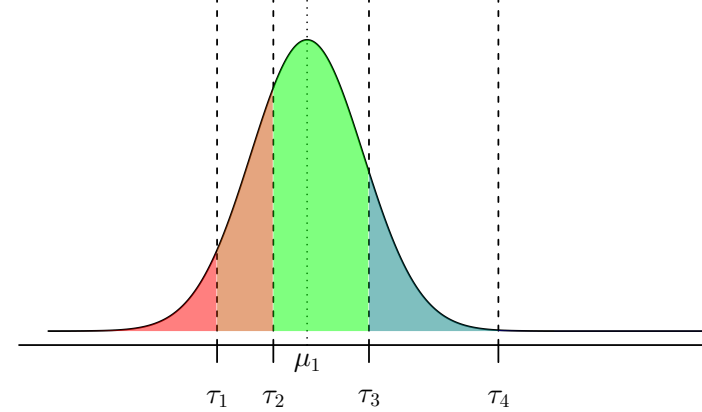
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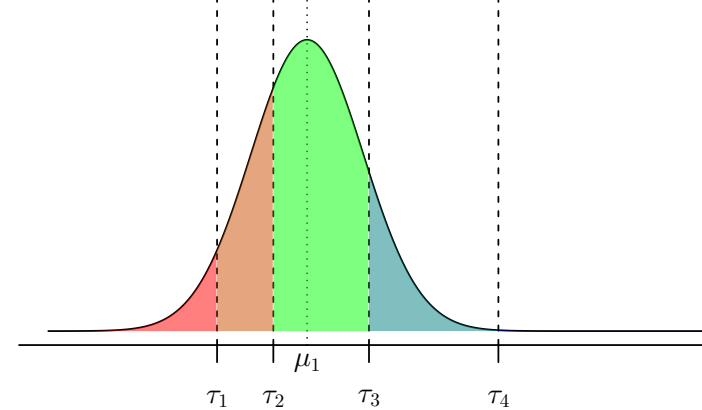
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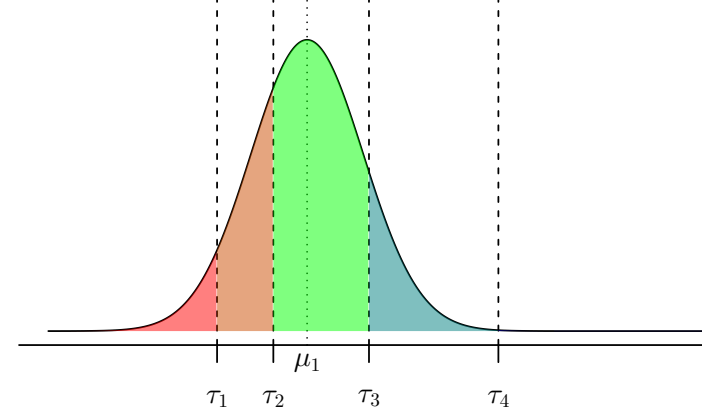


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- constrain cutoffs, e.g. $\tau_1 = 0$, or

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- constrain cutoffs, e.g. $\tau_1 = 0$, or
- drop intercept (that is what Stata does automatically)

Back to Hainmueller and Hiscox

To explicitly test the labor market competition argument, we estimate the systematic component of the ordered probit model with the specification.

$$\mu_i = \alpha + \gamma \text{HSKFRAME}_i + \delta (\text{HSKFRAME}_i \cdot \text{EDUCATION}_i) + \theta \text{EDUCATION}_i + Z_i \psi$$

where the parameter γ is the lower-order term on the treatment indicator that identifies the premium that natives attach to highly skilled immigrants relative to low-skilled immigrants. The parameter δ captures how the premium for highly skilled immigration varies conditional on the skill level of the respondent.



Z_i contains controls: 7 age bracket dummies, gender dummy, 4 race dummies

“Notice that because the randomization orthogonalized HSKFRAME with respect to Z , the exact covariate choice does not affect the results of the main coefficients of interest.” p.70

Hainmueller and Hiscox: ordered probit results

TABLE 1. Individual Support for Highly Skilled and Low-skilled Immigration—Test of the Labor Market Competition Model

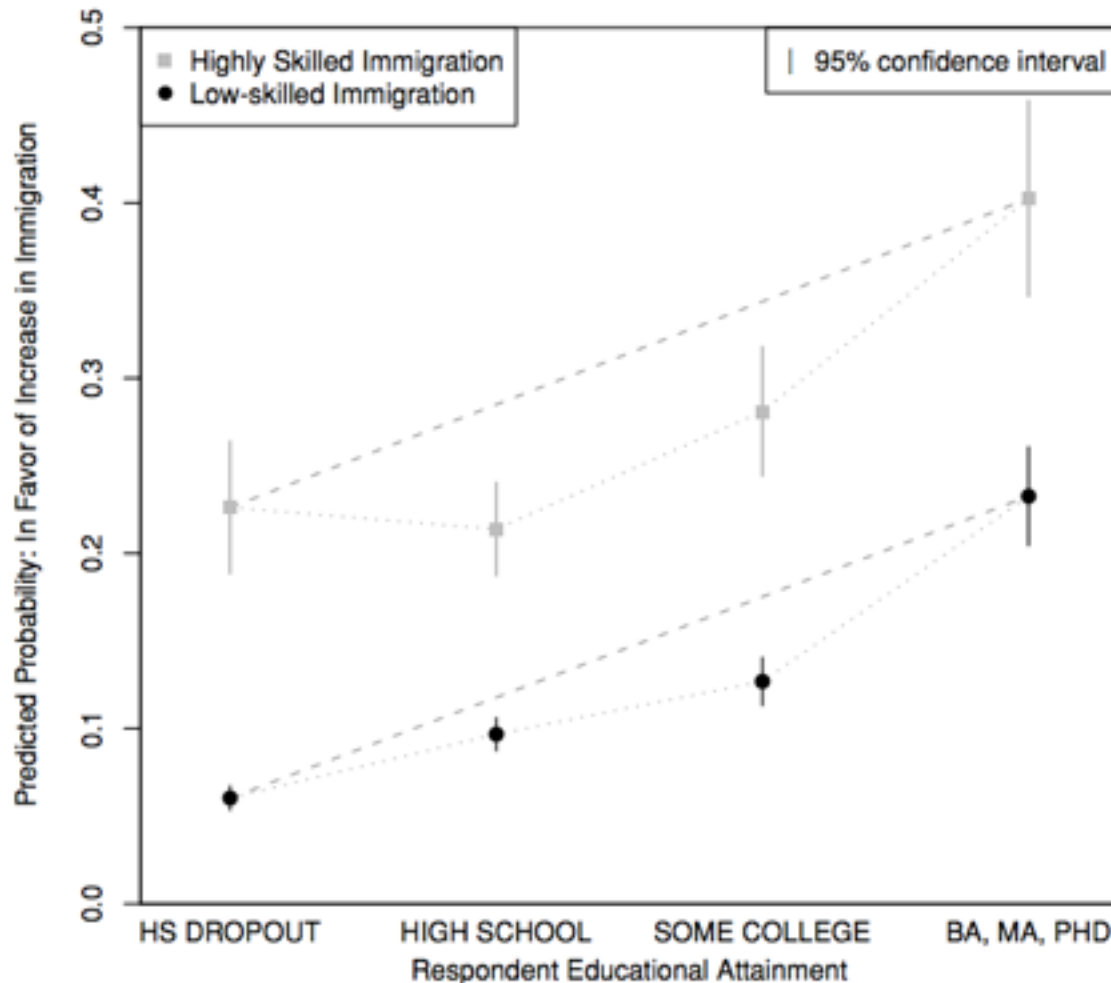
Dependent Variable	In Favor of:		In Favor of:				
	High Skilled Immigration	Low-skilled Immigration			Immigration	labor force	
	(1)	(2)	(3)	(4)	(5)	(6) in	(7) out
EDUCATION	0.21 (0.05)	0.27 (0.05)		0.27 (0.05)		0.33 (0.06)	0.19 (0.07)
HSKFRAME			0.54 (0.07)	0.73 (0.20)	0.56 (0.12)	0.73 (0.28)	0.64 (0.29)
HSKFRAME·EDUCATION				-0.07 (0.07)		-0.08 (0.09)	0.00 (0.11)
HS DROPOUT					-0.41 (0.18)		
HSKFRAME·HS DROPOUT					0.24 (0.25)		
HIGH SCHOOL					-0.16 (0.12)		
HSKFRAME·HIGH SCHOOL					-0.05 (0.17)		
BA DEGREE					0.41 (0.12)		
HSKFRAME·BA DEGREE					-0.08 (0.16)		
(N)	798	791	1589	1589	1589	946	643
Covariates	X	X	X	X	X	X	X

Order Probit Coefficients shown with standard errors in parentheses. All models include a set of the covariates age, gender, and race (coefficients not shown here). The reference category for the set of education dummies is SOME COLLEGE (respondents with some college education).

Hainmueller and Hiscox: logit results

To give some sense of the substantive magnitudes involved, we simulate the predicted probability of supporting an increase in immigration (answers “somewhat agree” and “strongly agree” that the U.S. should allow more immigration) for the median respondent (a white woman aged 45) for all four skill levels and both immigration types based on the least restrictive model (model five in Table 1).

FIGURE 4. Support for Highly Skilled and Low-skilled Immigration by Respondents' Skill Level



Hainmueller and Hiscox: presentation ACTIVITY!!!

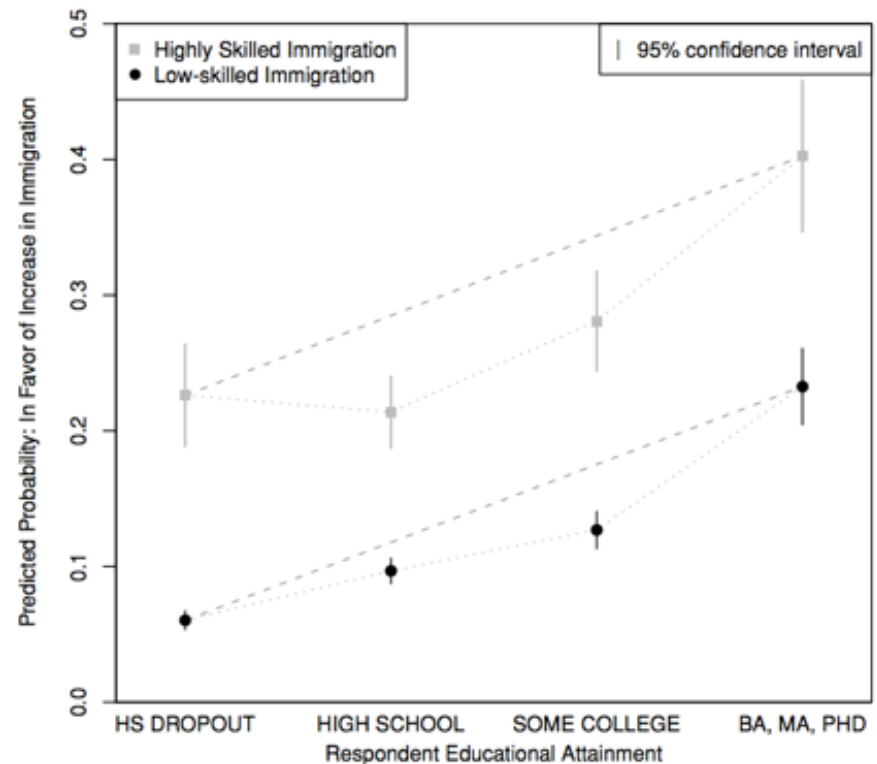
How could Hainmueller and Hiscox have graphically summarized the findings of their ordered probit regression (rather than switching to a binary outcome)?

TABLE 1. Individual Support for Low-skilled Immigration—Test Labor Market Competition

Dependent Variable	In Favor of: Immigration		
	(3)	(4)	(5)
EDUCATION		0.27 (0.05)	
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Covariates	X	X	X

Order Probit Coefficients shown wAll models include a set of the covariate race (coefficients not shown here). ¹ education dummies is SOME COLLEGI some college education).

Support for Highly Skilled and Low-skilled Immigration by Respondents' Si

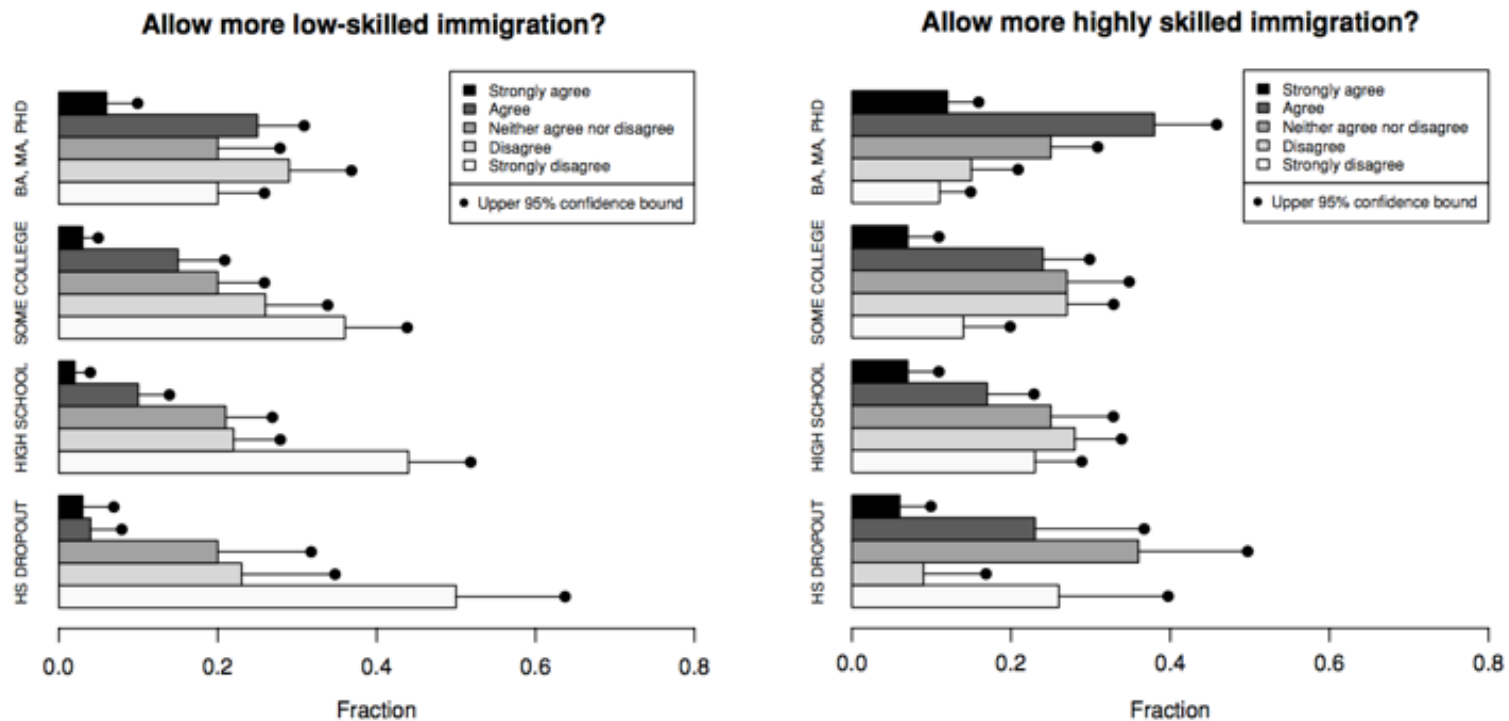


Hainmueller and Hiscox: presentation

SOLUTION?

One option: like Figure 3 but with predicted probabilities from the model.

FIGURE 3. Support for Highly Skilled and Low-skilled Immigration by Respondents' Skill Level



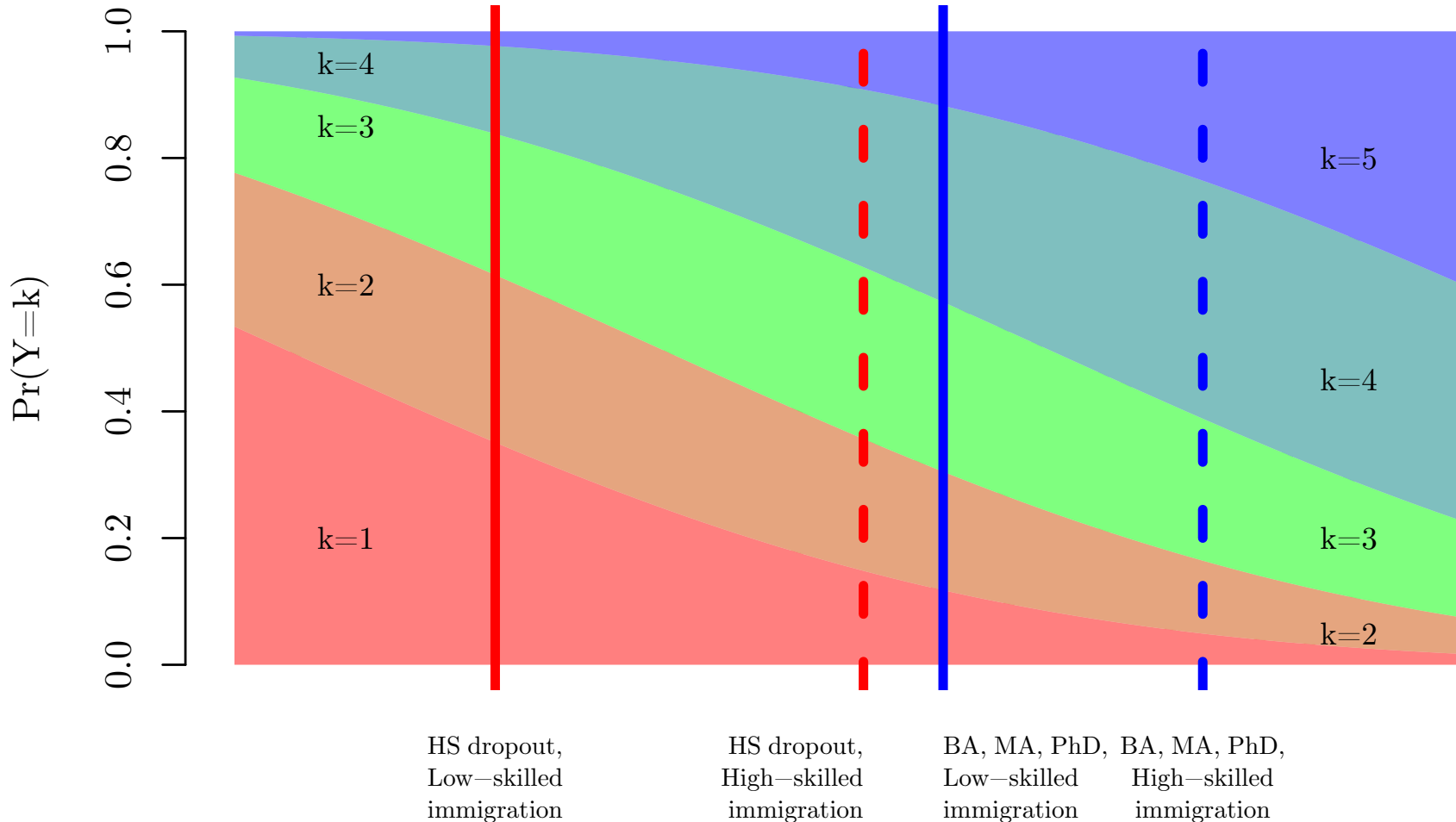
Hainmueller and Hiscox: presentation *SOLUTION?*

Another option: predicted probabilities at various values of $X\beta$, with some predicted values of $X\beta$ shown

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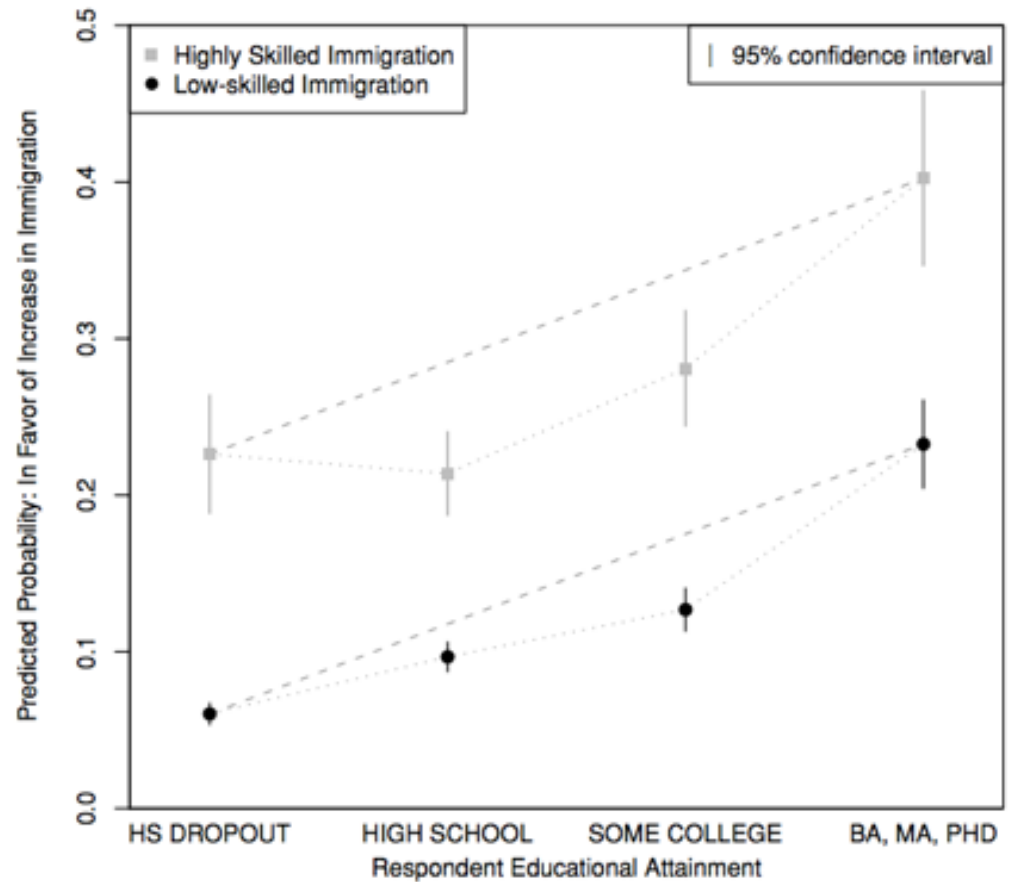


Why do we need logit?

ACTIVITY!!!

Consider H&H's logit analysis: support for more immigration (binary) as function of education, type of immigration.

Support for Highly Skilled and Low-skilled Immigration by Respondents' Si



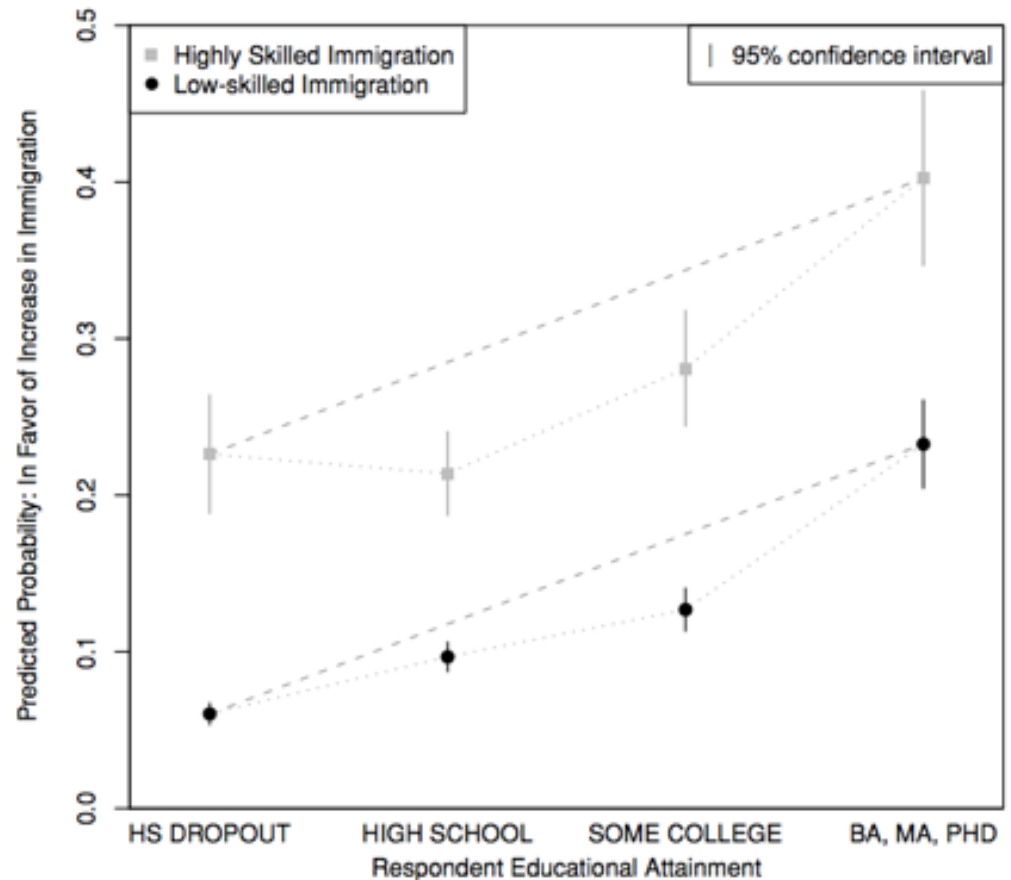
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Why not estimate a linear probability model (LPM)?

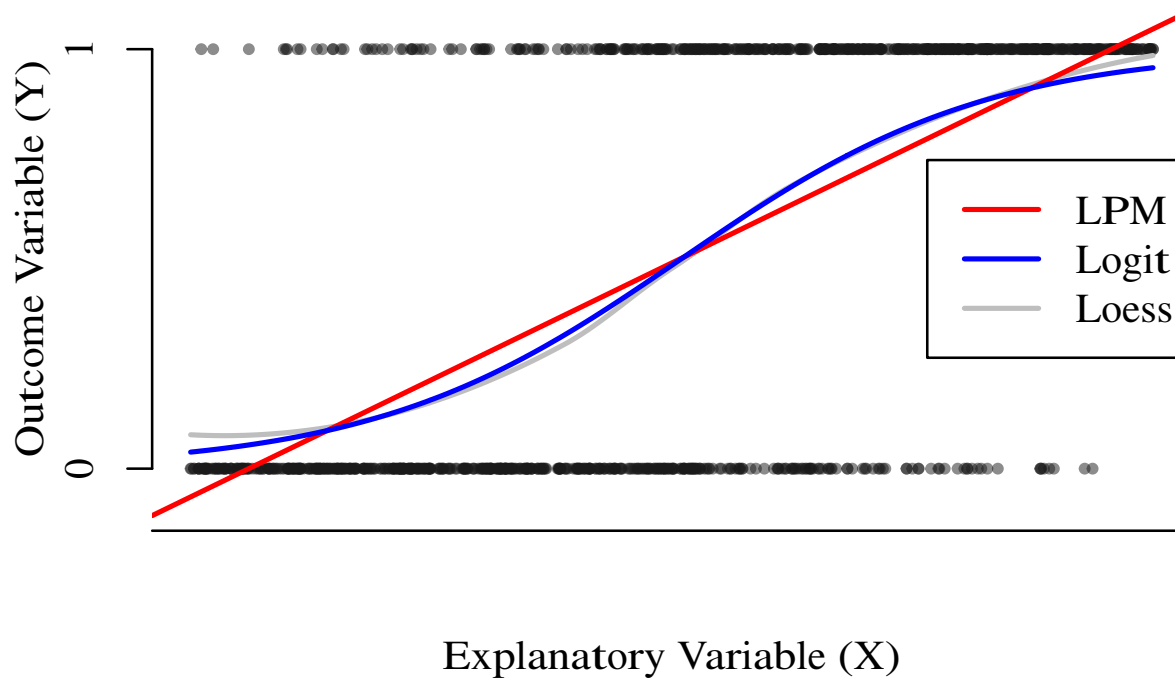
Support for Highly Skilled and Low-skilled Immigration by Respondents' Si



$$\text{SUPPORT}_i = \alpha + \gamma \text{HSKFRAME}_i + \delta \text{HSKFRAME}_i \times \text{EDUCATION}_i + \theta \text{EDUCATION}_i + Z_i \psi$$

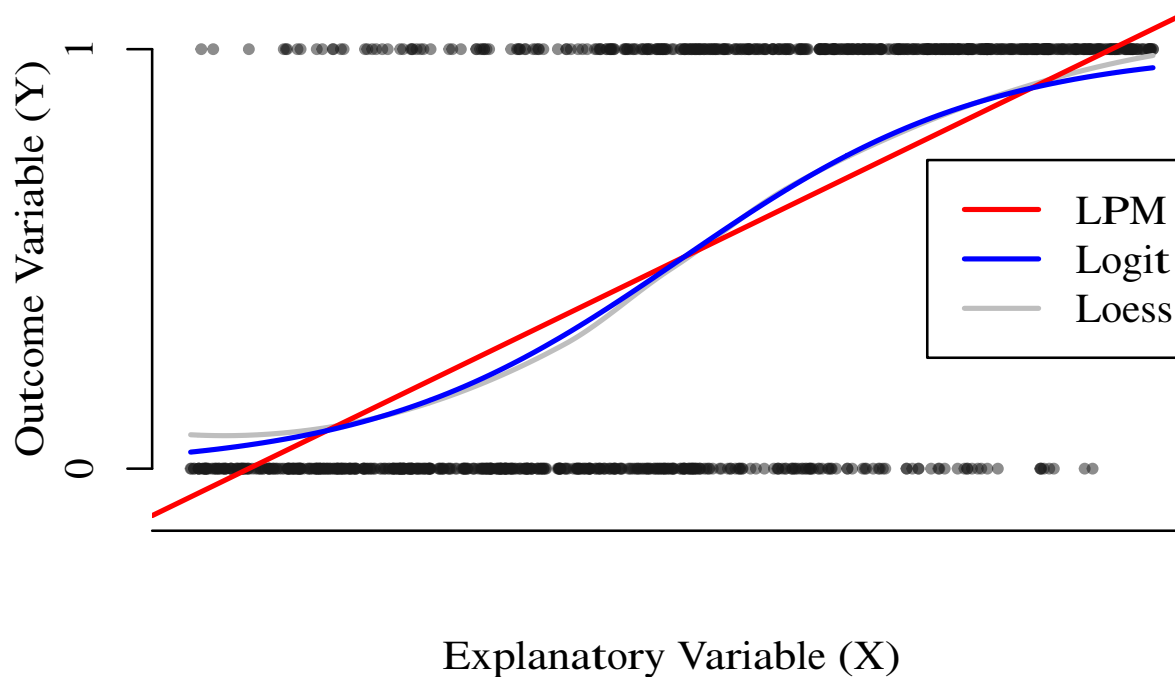
The usual case against the linear probability model (LPM)

SOLUTION?



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SOLUTION?



- *Predictions outside the range of dependent variable*
- *Heteroskedasticity (violates OLS assumption)*
- *Non-normal errors (violates OLS assumption)*
- *Unrealistic for probability to be linear in X*

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 - Yes, especially when probabilities are near 1 or 0 (ceiling and floor effects); but is probit the right form?

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SOLUTION?

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 - Logit vs LPM matters only if particular kind of covariate imbalance

The defense of the LPM: continued

SOLUTION?

Gailmard pp 171-2



“If the CEF is linear, as it is for a saturated model, [OLS] gives the CEF... If the CEF is non-linear, [OLS] approximates the CEF. Usually it does it pretty well. Obviously, the LPM won't give the true marginal effects from the right nonlinear model. But then, the same is true for the 'wrong' nonlinear model! The fact that we have a probit, a logit, and the LPM [shows] that we don't know what the 'right' model is. Hence, there is a lot to be said for sticking to a linear regression function as compared to a fairly arbitrary choice of a non-linear one! Nonlinearity per se is a red herring.”



Steve Pischke

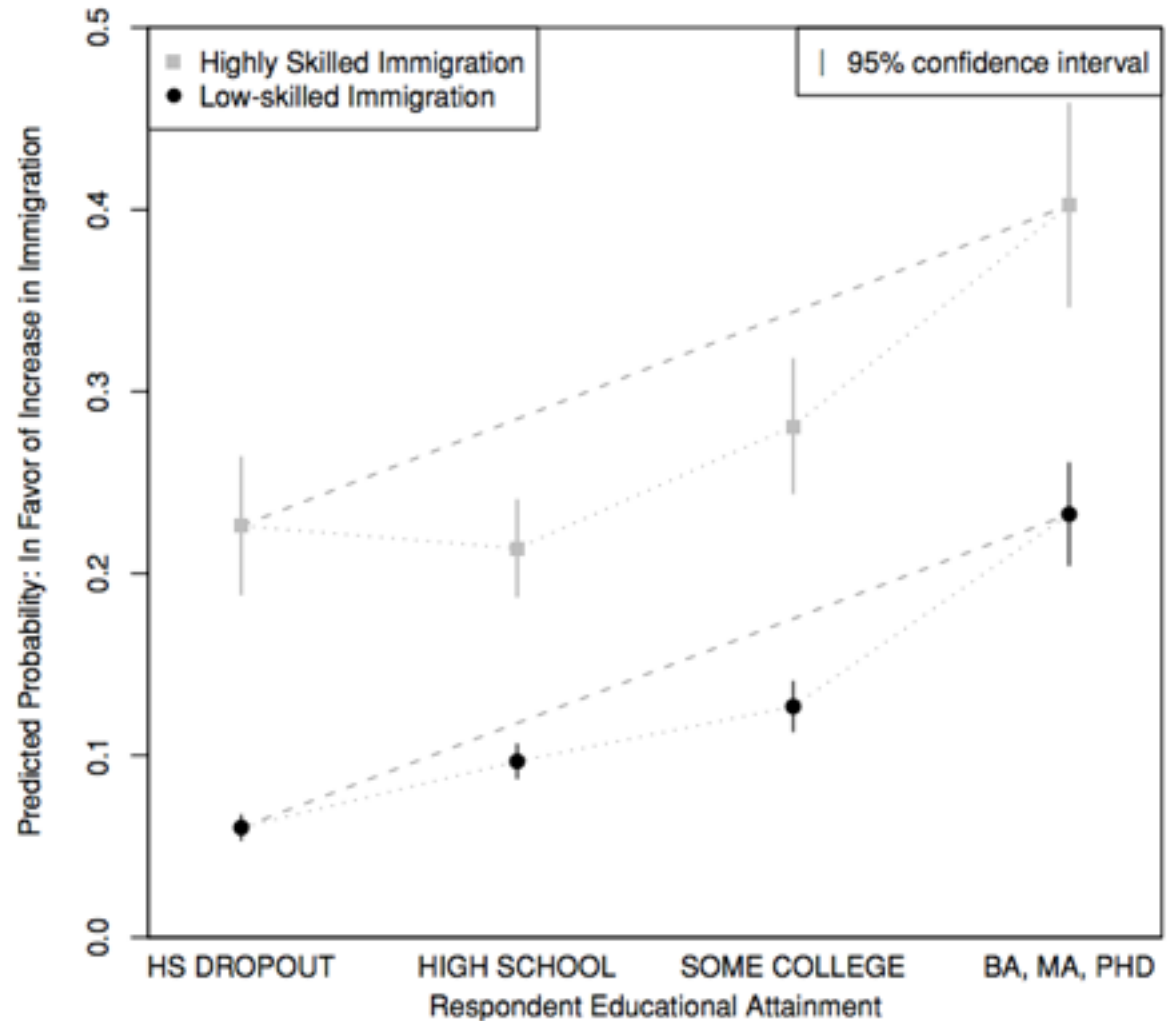
from MHE blog <http://www.mostlyharmlesseconometrics.com/2012/07/probit-better-than-lpm/>

The defense of the LPM: continued

SOLUTION?

Original Figure 4
(based on logit)

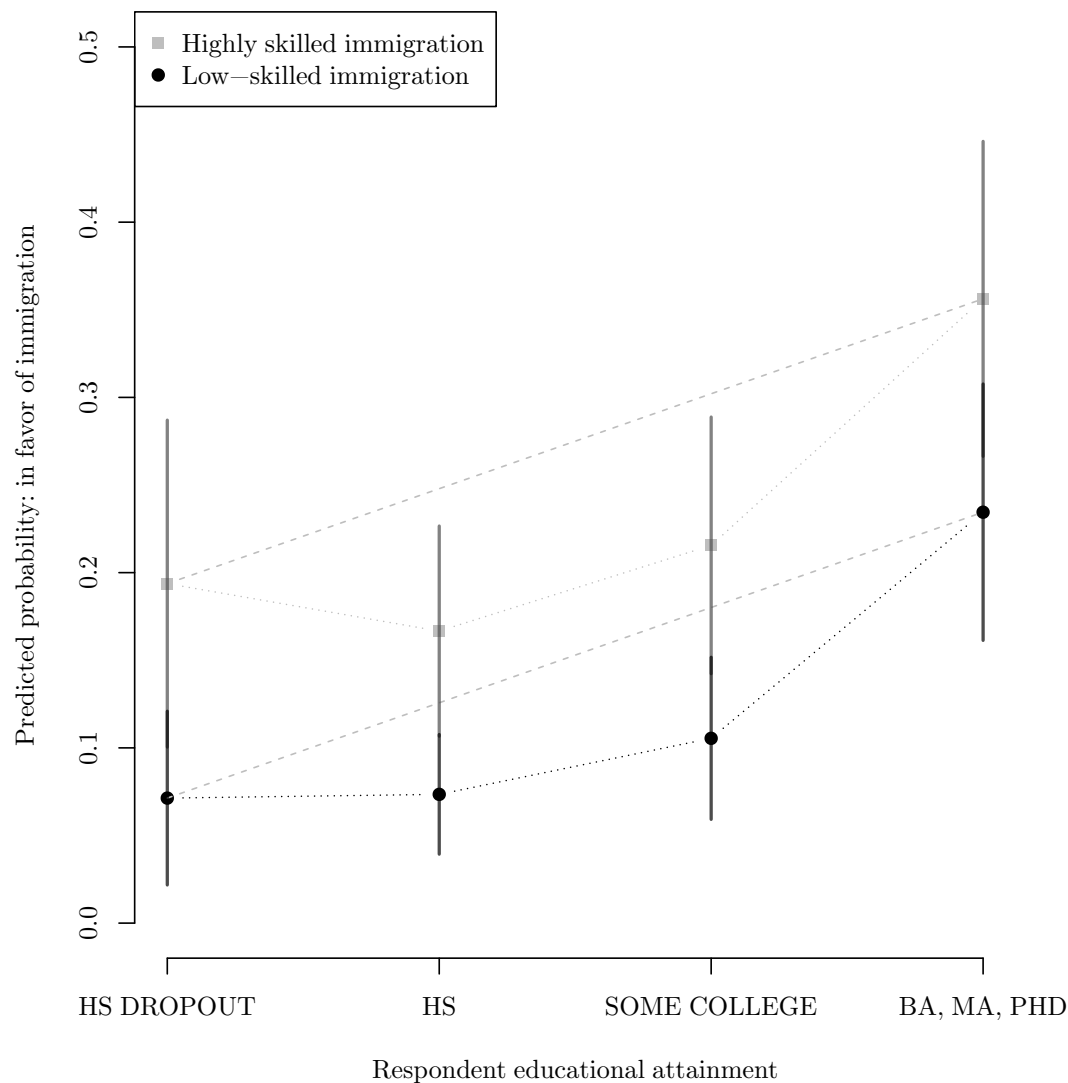
Support for Highly Skilled and Low-skilled Immigration by Respondents' Si



The defense of the LPM: continued

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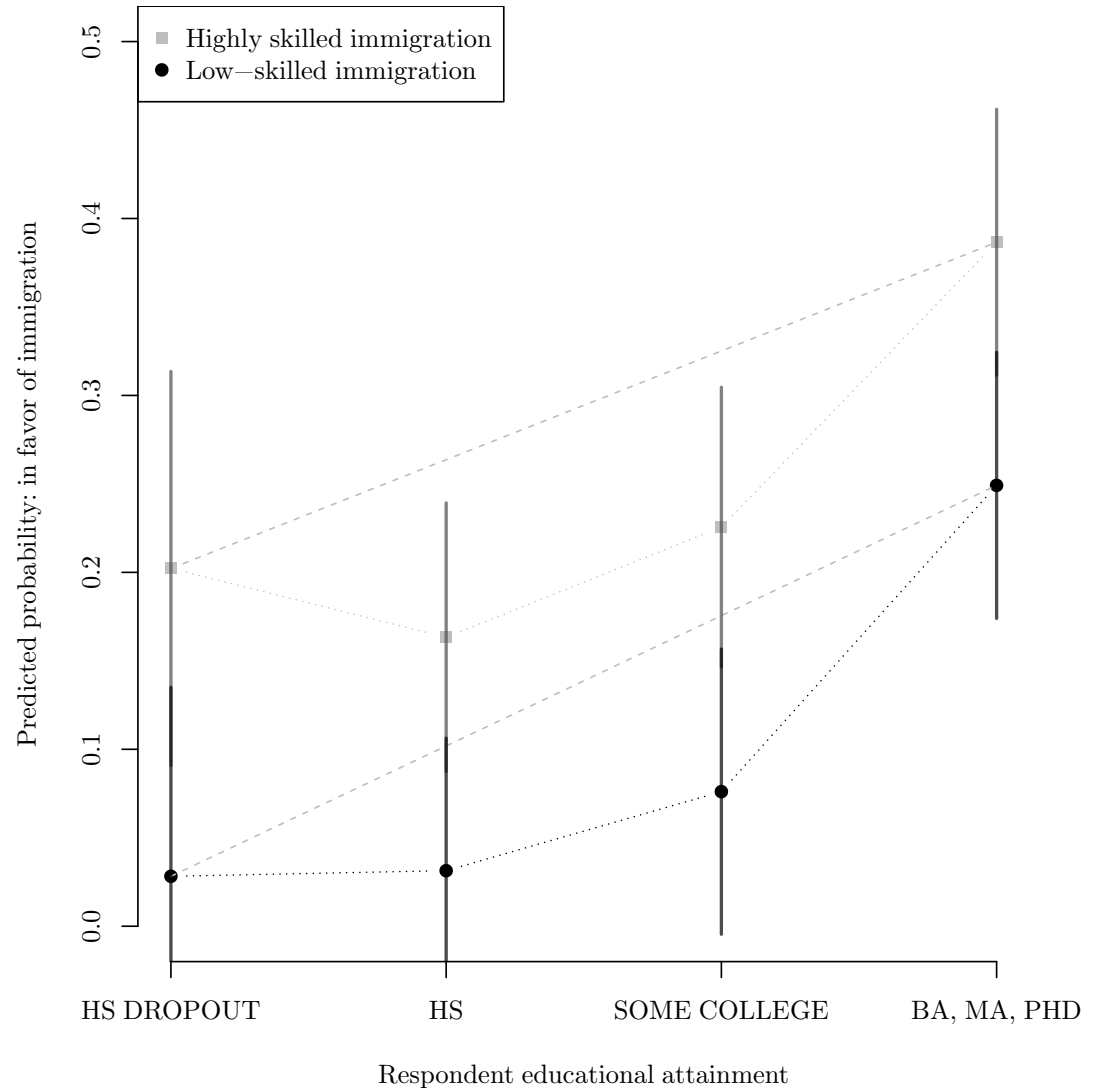
My Figure 4 (based on logit)



The defense of the LPM: continued

SOLUTION?

My Figure 4 (based on LPM)



Why do we need ordered probit?

ACTIVITY!!!

Consider H&H's ordered probit analysis: support for more immigration (five categories) as function of education, type of immigration.

Why do we need ordered probit?

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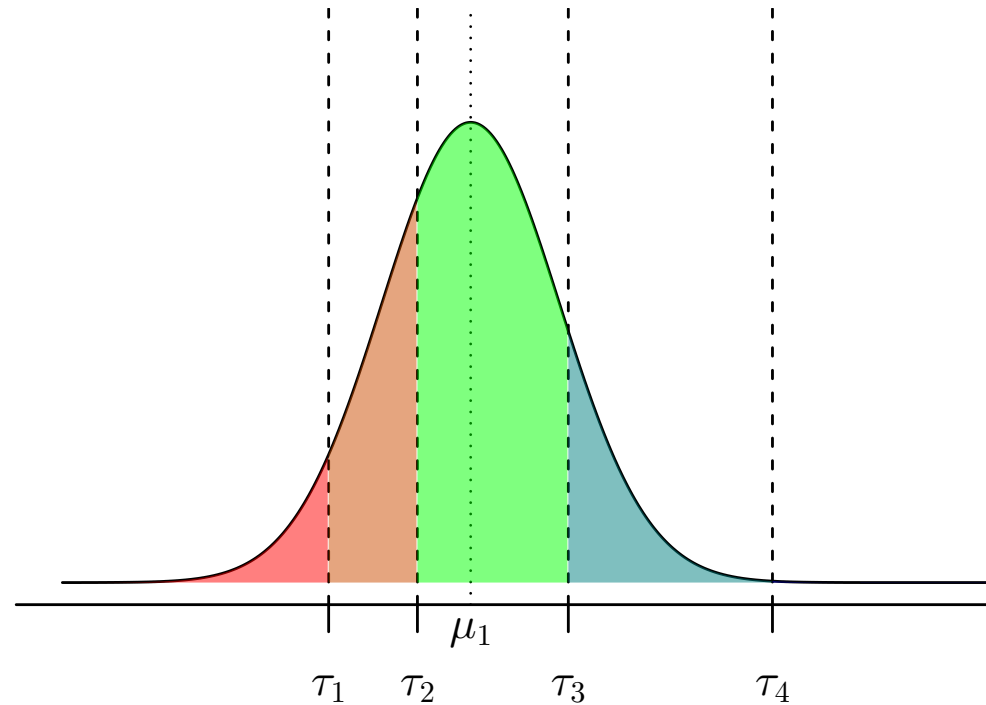
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Why not just estimate a **linear regression** where the DV is 1-5 scores?

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Consider H&H's ordered probit analysis: support for more immigration (five categories) as function of education, type of immigration.



Why not just estimate a **linear regression** where the DV is 1-5 scores?

Why do we need ordered probit?

SOLUTION?

- Some reviewers (still) ask for it
- Could produce predicted probabilities separately for each category
- Ceiling and floor effects: if nonlinearity is a problem in LPM, it could be here too
- More generally: outcome scores may not be linear in covariates

Introduction to measurement/scaling models

	Bill 1	Bill 2	Bill 3	...
Legislator 1	Y	Y		...
Legislator 2	Y	N	N	...
Legislator 3		N	N	...
Legislator 4	Y	Y	Y	...
...

Introduction to measurement/scaling models

Suppose we had voting data like that. What could you do with it?

	Bill 1	Bill 2	Bill 3	...
Legislator 1	Y	Y		...
Legislator 2	Y	N	N	...
Legislator 3		N	N	...
Legislator 4	Y	Y	Y	...
...

	Word 1	Word 2	Word 3	...
Article 1	0	14	2	...
Article 2	1	8	0	...
Article 3	0	7	1	...
Article 4	2	3	0	...
...

Or text data like that. What could you do with it?

	Word 1	Word 2	Word 3	...
Article 1	0	14	2	...
Article 2	1	8	0	...
Article 3	0	7	1	...
Article 4	2	3	0	...
...

	Candidate1	Candidate2	Candidate3	...
Interest group 1	0	\$5,000	0	...
Interest group 2	\$1,000	\$1,000	0	...
Interest group 3	0	0	\$10,000	...
Interest group 4	\$500	0	0	...
...

Or political contribution data like that. What could you do with it?

	Candidate1	Candidate2	Candidate3	...
Interest group 1	0	\$5,000	0	...
Interest group 2	\$1,000	\$1,000	0	...
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Common structure

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Data is grouped:

- many legislators, many bills
- many speakers, many words.

Though it probably didn't come in that format originally!

	these	that	those
Article 1	0	14	2
Article 2	1	8	0
Article 3	0	7	1
Article 4	2	3	0

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Article 4	2	3	0

Article 1: That that "that" that. That that those; that that that that. That that that that those.

Article 2: That that/these that that! That that that.

Article 3: That that those — that that that that that.

Article 4: These that! These that that.

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Article	Word	Count
1	these	0
2	these	1
3	these	0
4	these	2
1	that	14
2	that	8
3	that	7
4	that	3
1	those	2
2	those	0
3	those	1
4	those	0

A simpler example

ACTIVITY!!!

	Vote on Bill 2	X (Ideology score)
Legislator 1	1	34
Legislator 2	0	67
Legislator 3	0	49
Legislator 4	1	12
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What would this tell you?

A: Regress vote on x .

- LPM: $\alpha + \beta x_i$ is the predicted probability conditional on x_i
- Probit: $\Phi(\alpha + \beta x_i)$ (Normal CDF) is the predicted probability conditional on x_i
- Logit: $\alpha + \beta x_i$ is the log odds conditional on x_i

A slightly less simple example

ACTIVITY!!!

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...

Regress vote on

- x (ideology score)
- a dummy (indicator variable) for each bill, and
- the interactions between x and the bill dummies.

Result is a intercept α_j and slope β_j for each bill.

- LPM: $\alpha_j + \beta_j x_i$ is the predicted probability legislator i would vote for bill j
- Probit and Logit: same pattern as previous (simple) example

What does β_j tell you?

Doing the seemingly impossible

ACTIVITY!!!

	Bill	Vote	X (Ideology score)
Legislator 1	2	1	?
Legislator 2	2	0	?
Legislator 3	2	0	?
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...
Legislator 1	1	1	?
Legislator 2	1	1	?
Legislator 3	1		?
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...

Doing the seemingly impossible

ACTIVITY!!!

Now suppose the ideology score was missing. What now?

	Bill	Vote	X (Ideology score)
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Legislator 2	2	0	?
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...

Statistical model is the same as if x was observed, but x becomes an additional parameter to estimate.

This works because the same legislator votes on many bills; x is estimated based on recurring patterns of voting behavior.

The (generative) statistical model: same as probit

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Let $y_{ij} \in \{0, 1\}$ indicate i 's vote on bill j .

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Then

$$\Pr(y_{ij} = 1) = \Phi(\alpha_j + \beta_j x_i)$$

where $\Phi(\cdot)$ is the standard normal CDF.

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But imagine making guesses for α_j , β_j , and x_i . Because each x_i appears many times in the likelihood (i.e. the same legislator votes on many bills), some guesses would be better than others (i.e. would yield a higher value for the likelihood). Maximize the likelihood!

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A: $n \times k$

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Solution: various constraints (e.g. “Corbyn’s x_i must be negative, and the standard deviation of the x_i values must be 1.”)

Estimation (3)

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CRAN Task View: Psychometric Models and Methods

Maintainer: Patrick Mair

Contact: mair at fas.harvard.edu

Version: 2016-01-31

Psychometrics is concerned with theory and techniques of psychological measurement. Psychometricians have also worked collaboratively with those in the field of statistics and quantitative methods to develop improved ways to organize, analyze, and scale corresponding data. Since much functionality is already contained in base R and there is considerable overlap between tools for psychometry and tools described in other views, particularly in [SocialSciences](#), we only give a brief overview of packages that are closely related to psychometric methodology.

[Please let me know](#) if I have omitted something of importance, or if a new package or function should be mentioned here.

Item Response Theory (IRT):

- The [eRm](#) package fits extended Rasch models, i.e. the ordinary Rasch model for dichotomous data (RM), the linear logistic test model (LLTM), the rating scale model (RSM) and its linear extension (LRSM), the partial credit model (PCM) and its linear extension (LPCM) using conditional ML estimation. Missing values are allowed.
- The package [ltm](#) also fits the simple RM. Additionally, functions for estimating Birnbaum's 2- and 3-parameter models based on a marginal ML approach are implemented as well as the graded response model for polytomous data, and the linear multidimensional logistic model.
- [TAM](#) fits unidimensional and multidimensional item response models and also includes multifaceted models, latent regression models and options for drawing plausible values.
- The [mirt](#) allows for the analysis of dichotomous and polytomous response data using unidimensional and multidimensional latent trait models under the IRT paradigm. Exploratory and confirmatory models can be estimated with quadrature (EM) or stochastic (MHRM) methods. Confirmatory bi-factor and two-tier analyses are available for modeling item testlets. Multiple group analysis and mixed effects designs also are available for detecting differential item functioning and modelling item and person covariates.
- [IRTShiny](#) provides an interactive shiny application for IRT analysis.
- The [mcIRT](#) package provides functions to estimate the Nominal Response Model and the Nested Logit Model. Both are models to examine multiple-choice items and other polytomous response formats. Some additional uni- and multidimensional item response models (especially for locally dependent item responses) and some exploratory methods (DETECT, LSDM, model-based reliability) are included in [sirt](#).
- The [pcIRT](#) estimates the multidimensional polytomous Rasch model and the Mueller's continuous rating scale model.
- Thurstonian IRT models can be fitted with the [kciRT](#) package.
- [MultiLCIRT](#) estimates IRT models under (1) multidimensionality assumption, (2) discreteness of latent traits, (3) binary and ordinal polytomous items.
- Conditional maximum likelihood estimation via the EM algorithm and information-criterion-based model selection in

Use of scaling models beyond legislative voting

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- Measuring student ability and question difficulty in educational testing (origin of item response theory)

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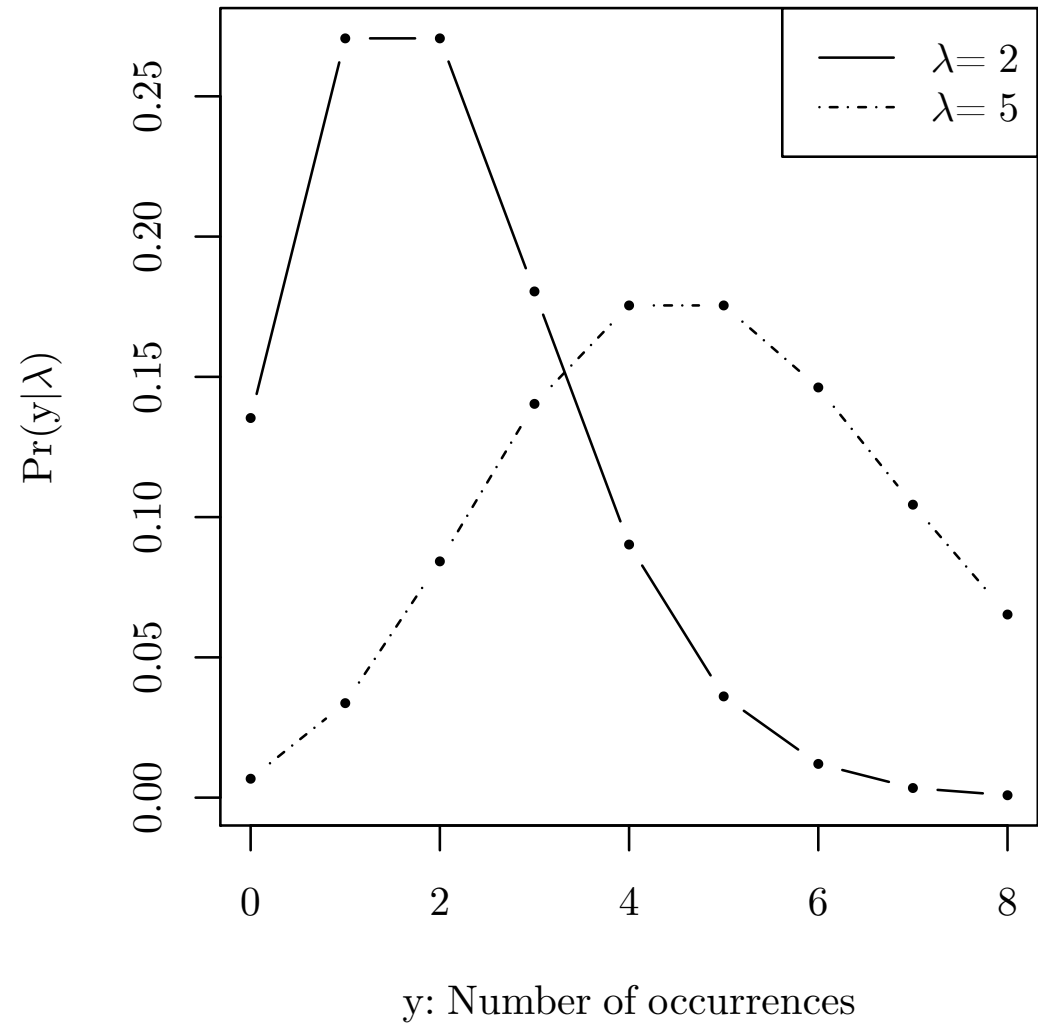
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- Measuring judges' ideology and how it changes over time (Martin & Quinn)

Scaling text: wordfish

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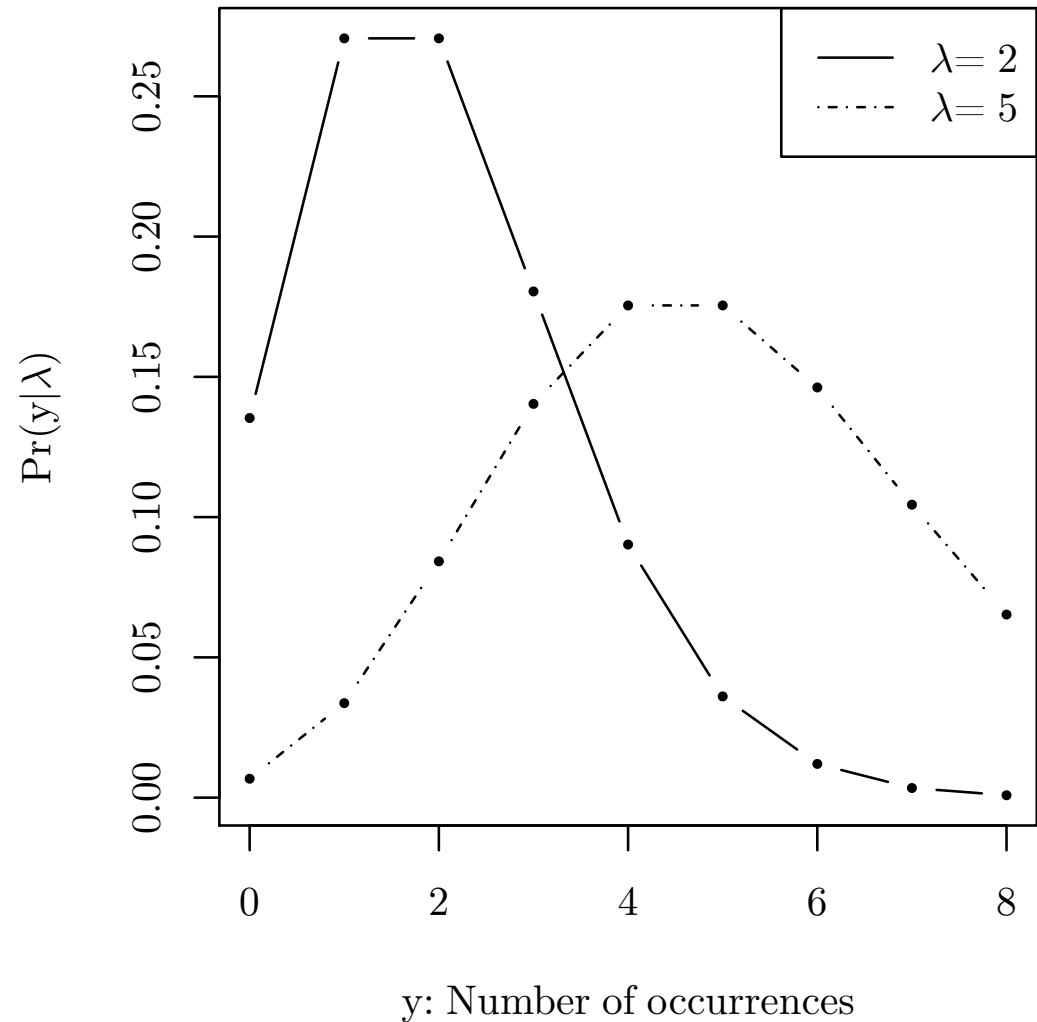
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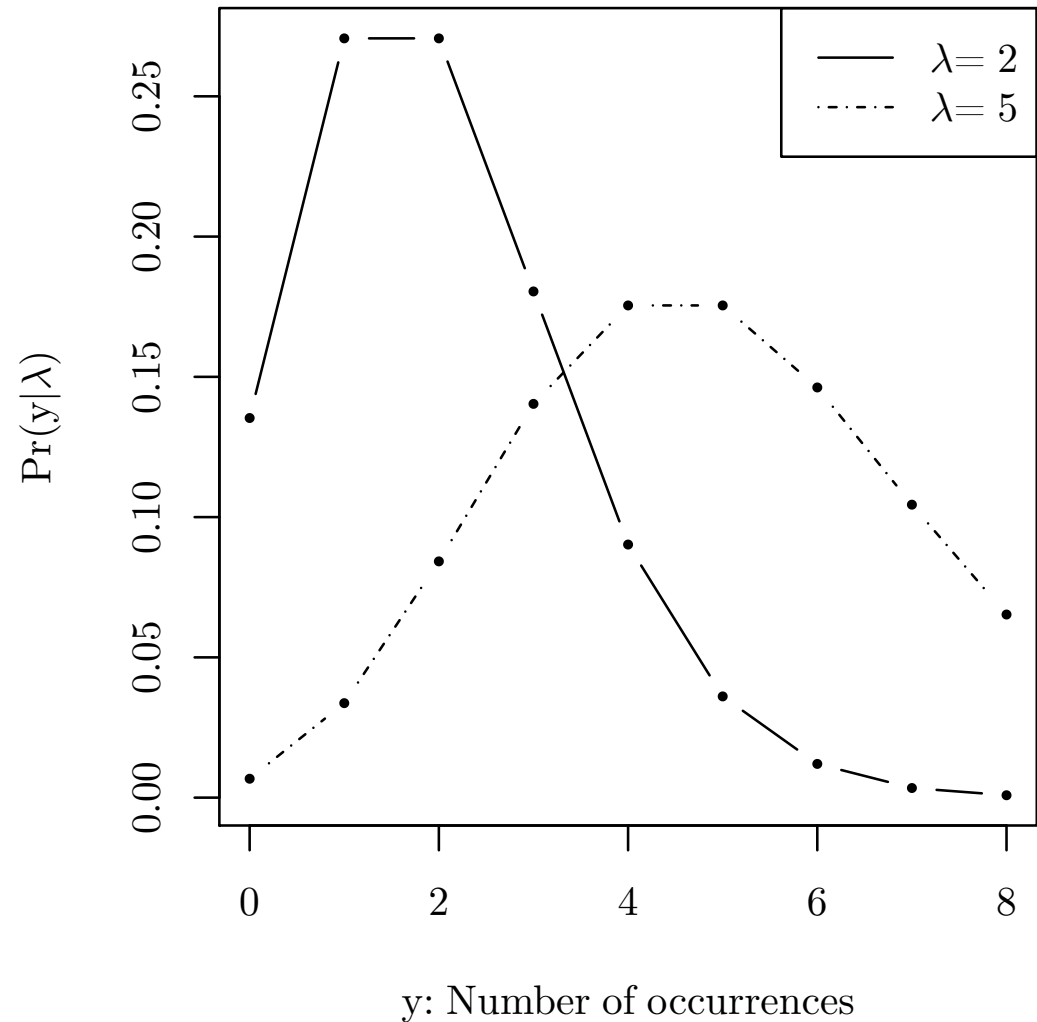
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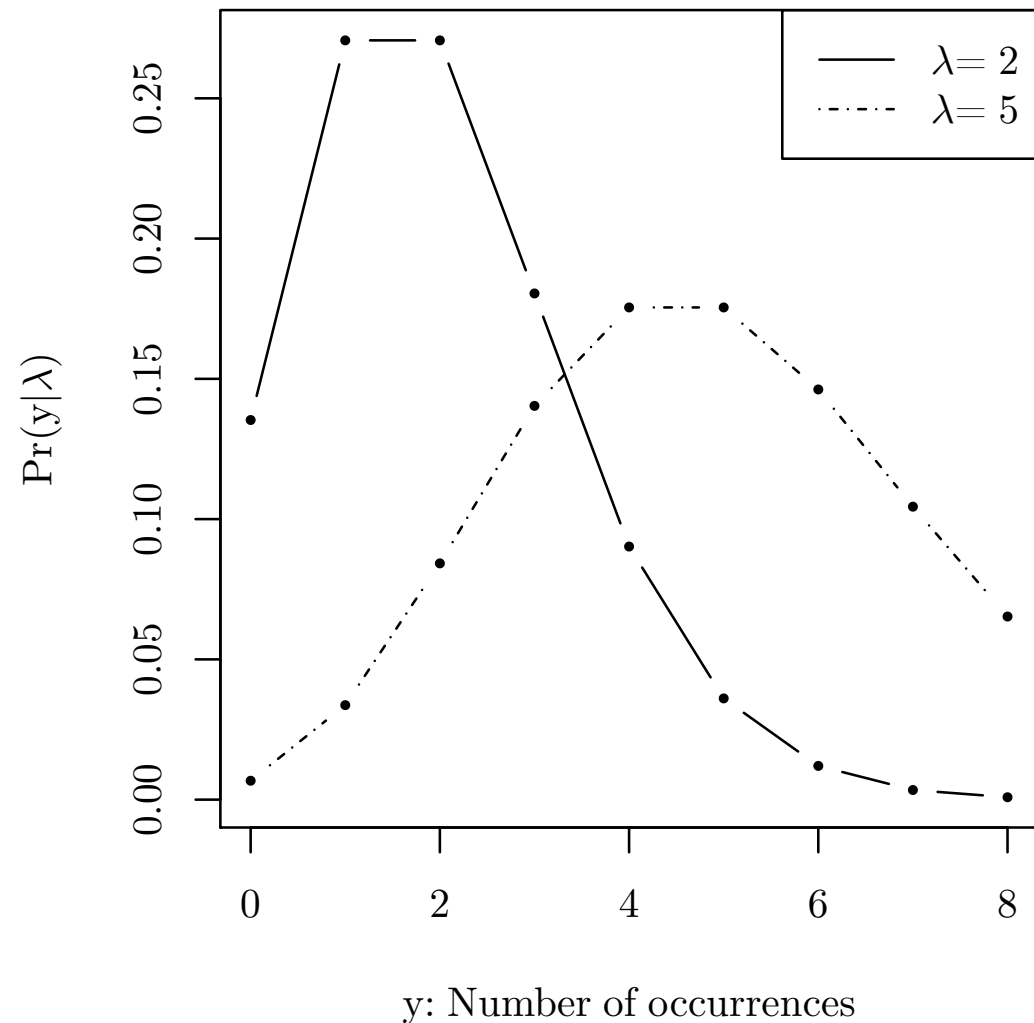
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Consider this model for the rate λ for party i using word j at time t :

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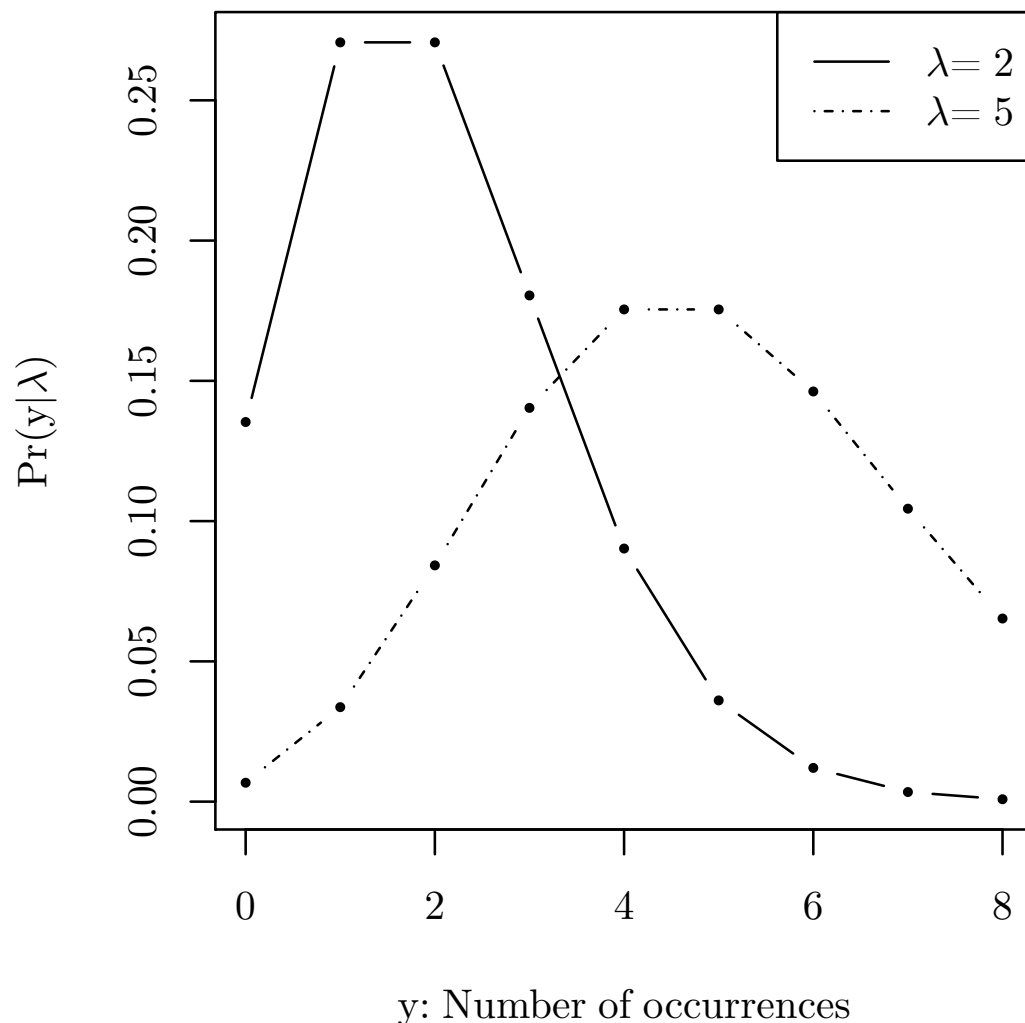
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- ω_{it} is party i 's position in year t



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Q: What values of ψ_j and β_j would you expect for these words?

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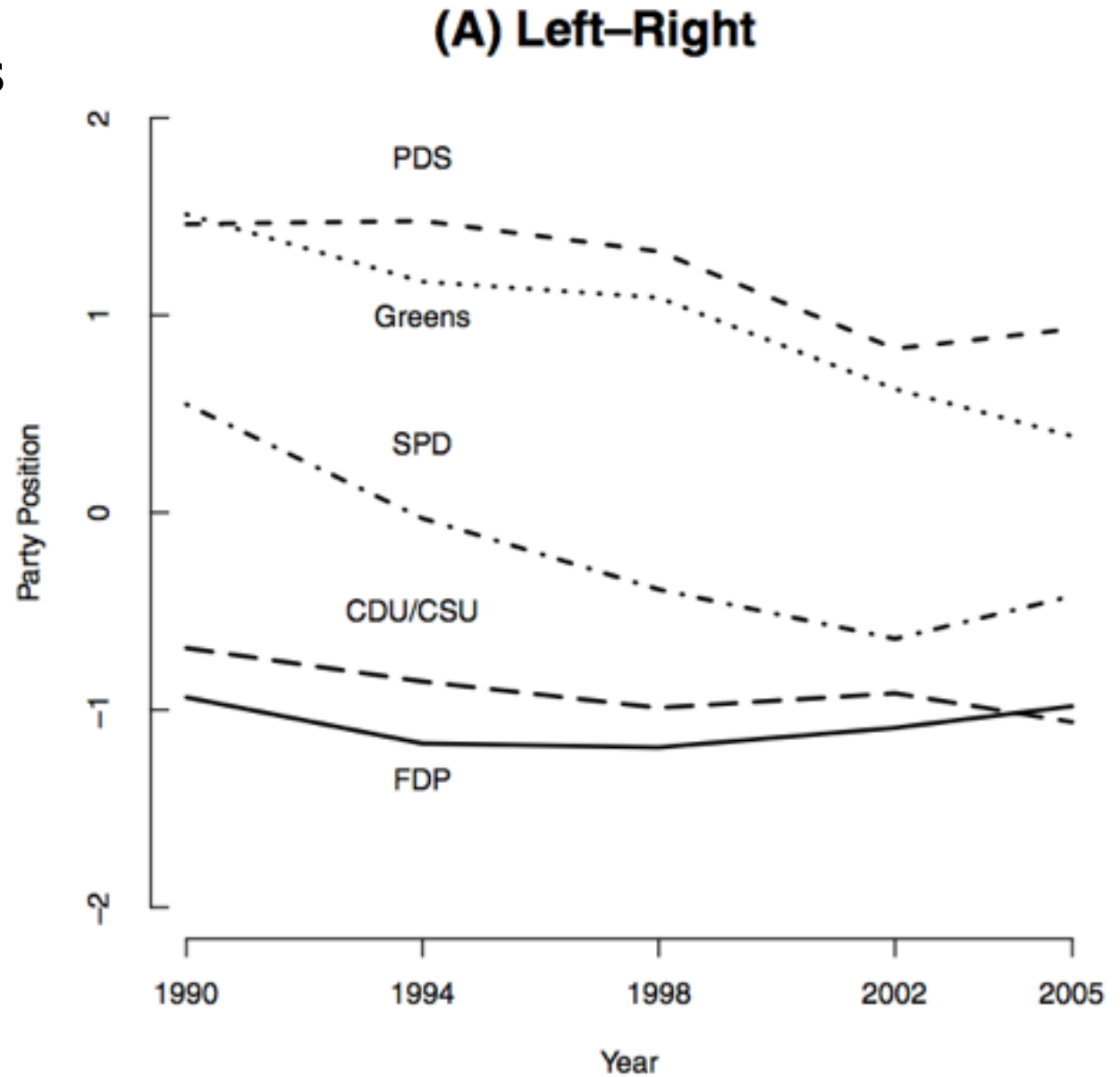
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For the word “deficit”:

- lower ψ_j
- larger (in magnitude) β_j ; for example, if the right talks about “deficits” more frequently and party positions are oriented so that right is positive, β_j should be large and positive.

Estimated party positions in Germany

Slapin and Proksch, 2008



Variations to be aware of

The underlying model:

- In IRT approaches, behavior is monotonic in x_i : the further right you are, the more likely you are to vote for a conservative measure
- In other approaches (e.g. Bonica 2013 on PAC contributions; Solomon and Messing 2015 on Facebook likes), behavior depends on proximity: the closer I am to the candidate the more likely I am to contribute/like

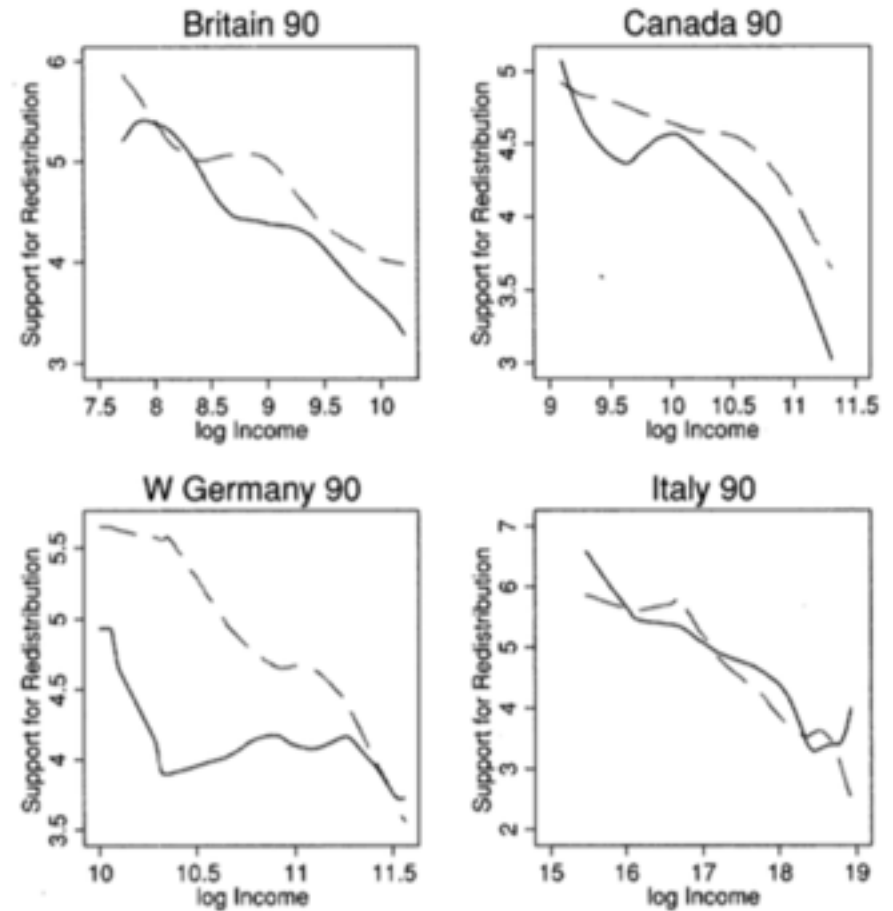
Level of aggregation:

- Classic uses are about estimating x for each individual: student ability, legislator ideology, etc
- Caughey and Warshaw 2015 estimate a group-level x based on sparse survey data

Other interesting uses of statistical modeling

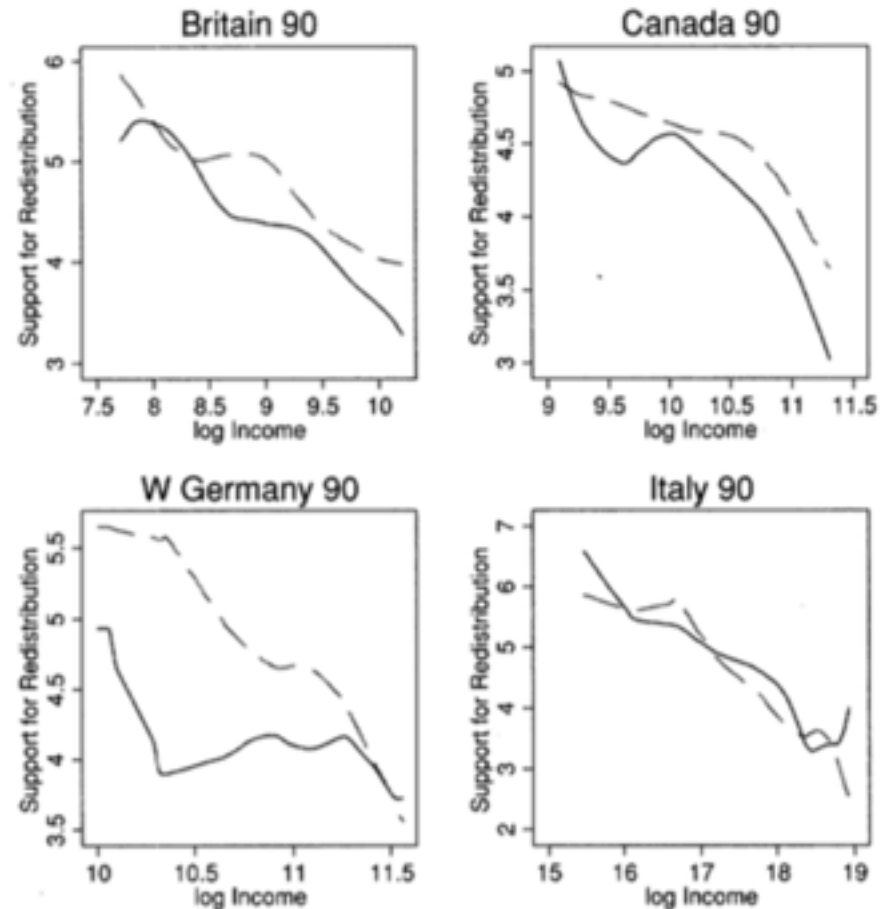
- “Small-area estimation”: How can we estimate the average preference of each legislative district (e.g. on same-sex marriage) with a survey that only has 5-10 respondents per district? (**MRP**: Multilevel regression and post-stratification)
- Topic modeling in text: what “topics” are being discussed in a corpus? How much does each document participate in each topic?

You can say a lot without a statistical model!



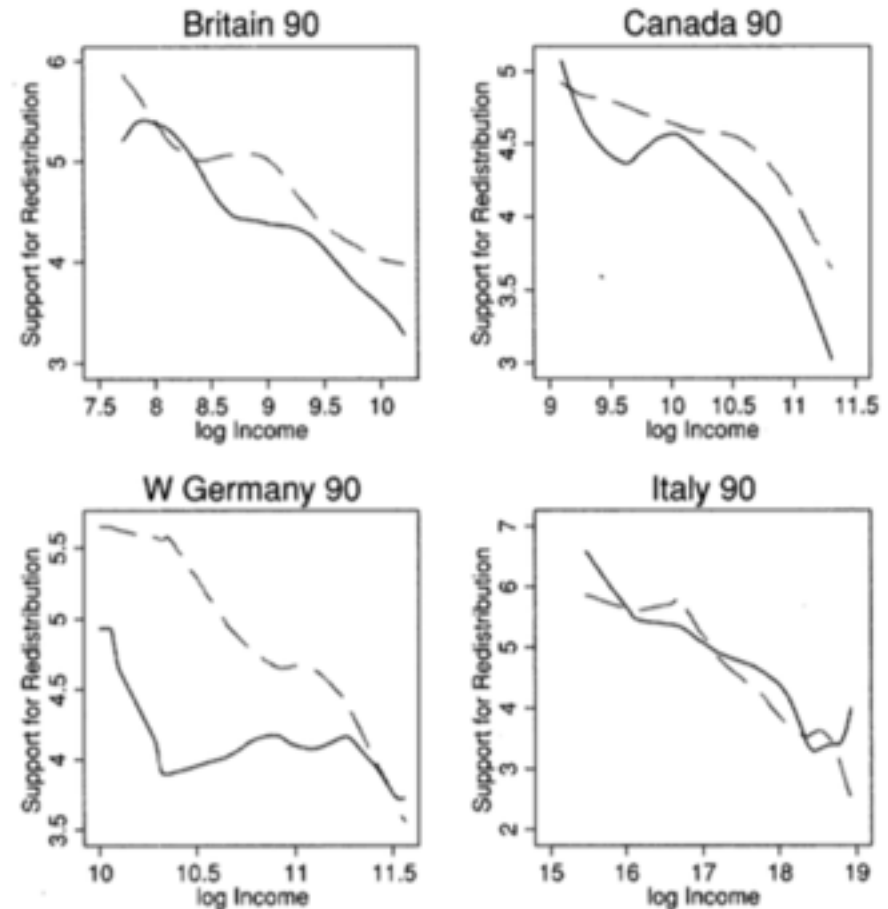
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At right: Kernel regressions of support for redistribution as function of income for WVS respondents who were “Very Proud” and “Less Proud” of their country



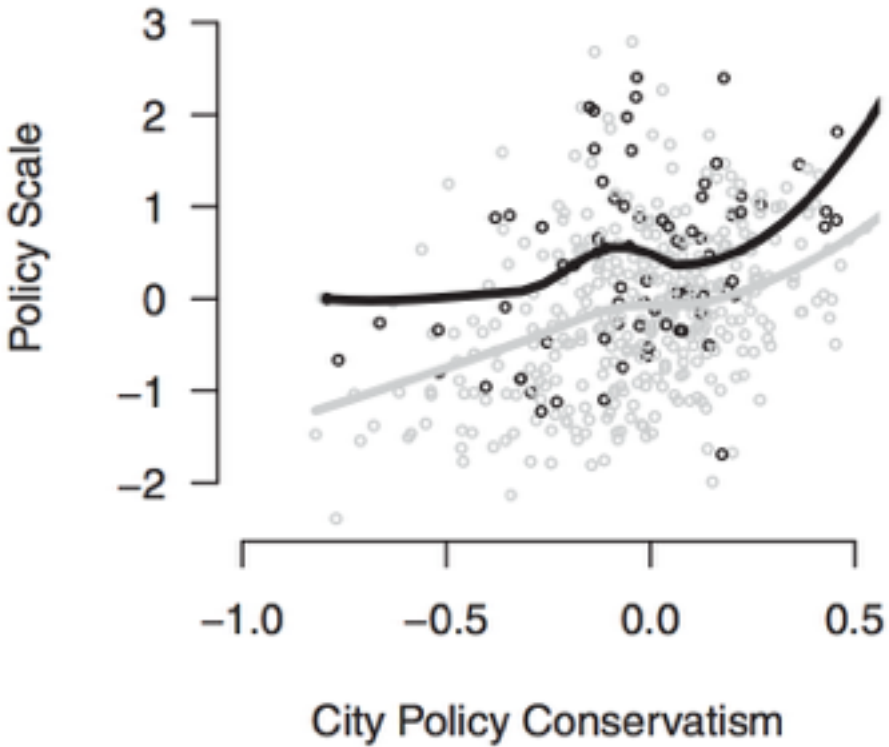
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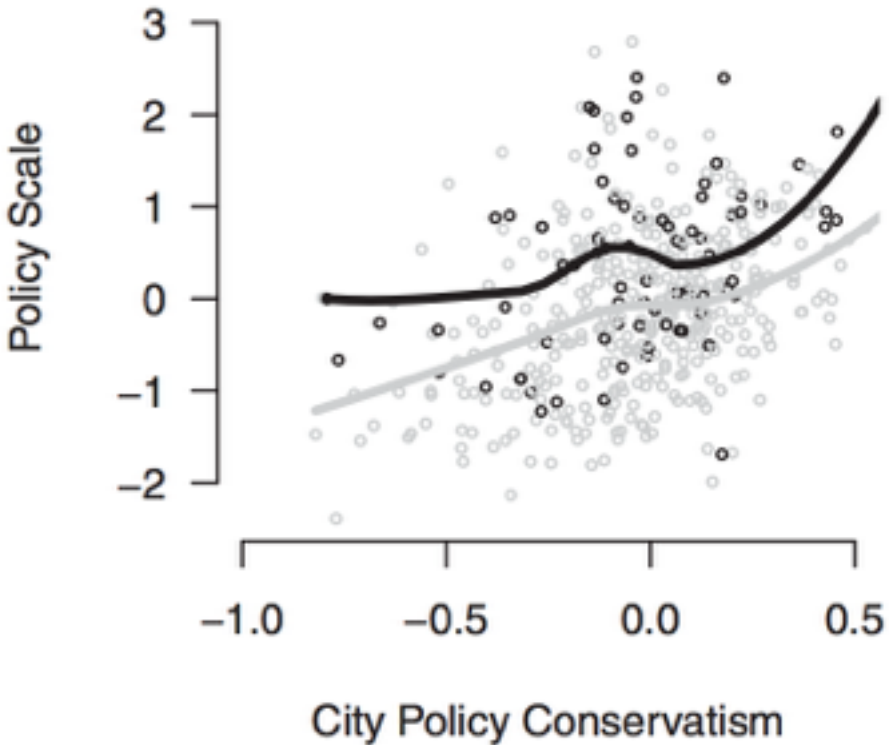


Shayo (2009) “A model of social identity” APSR.

And the best statistics are easy to miss

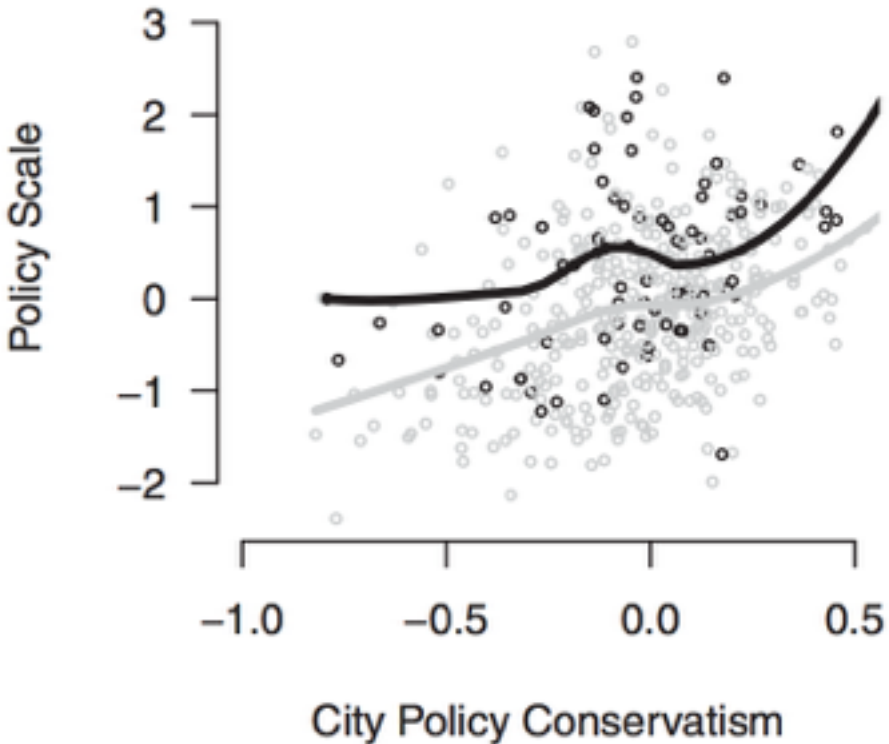


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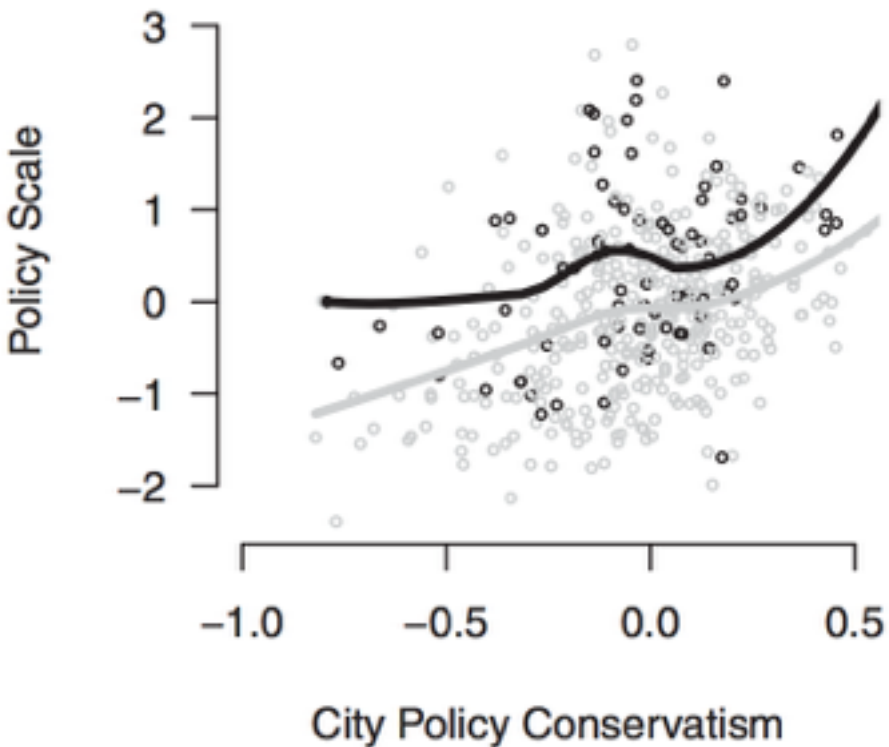
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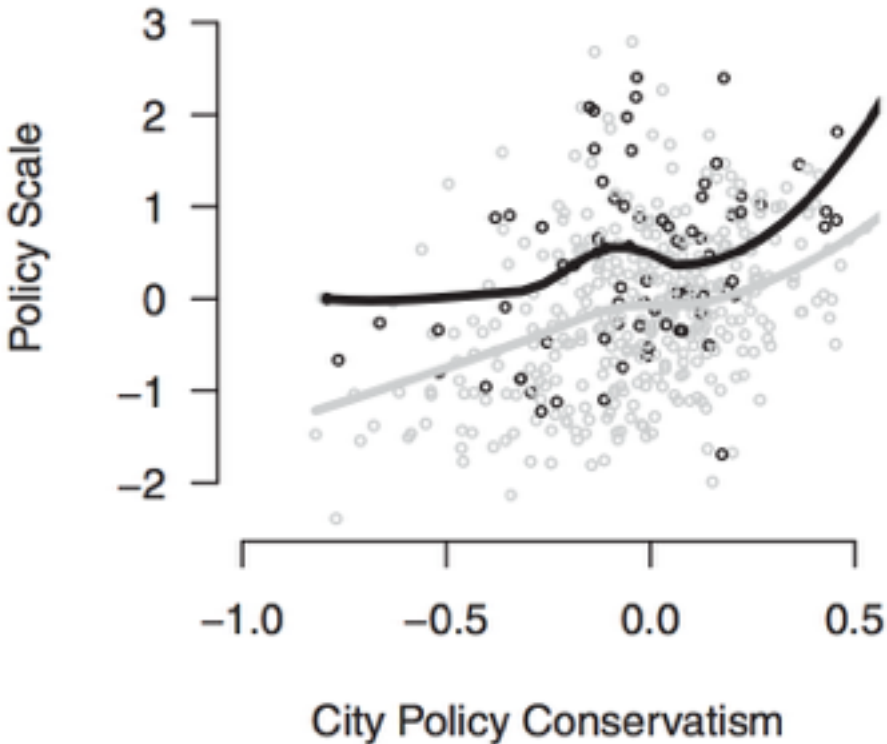
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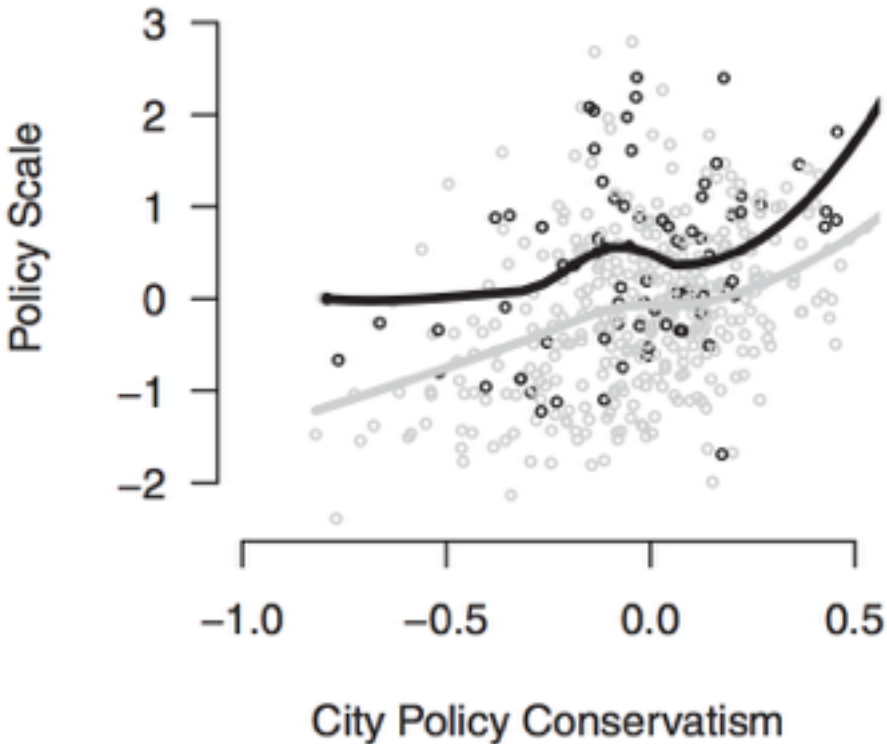
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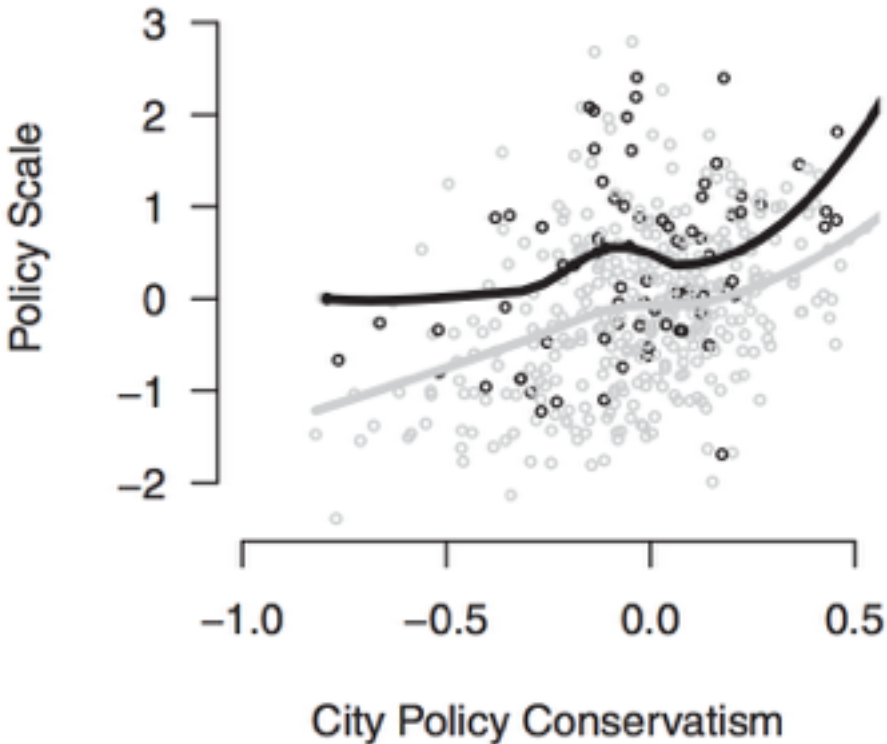
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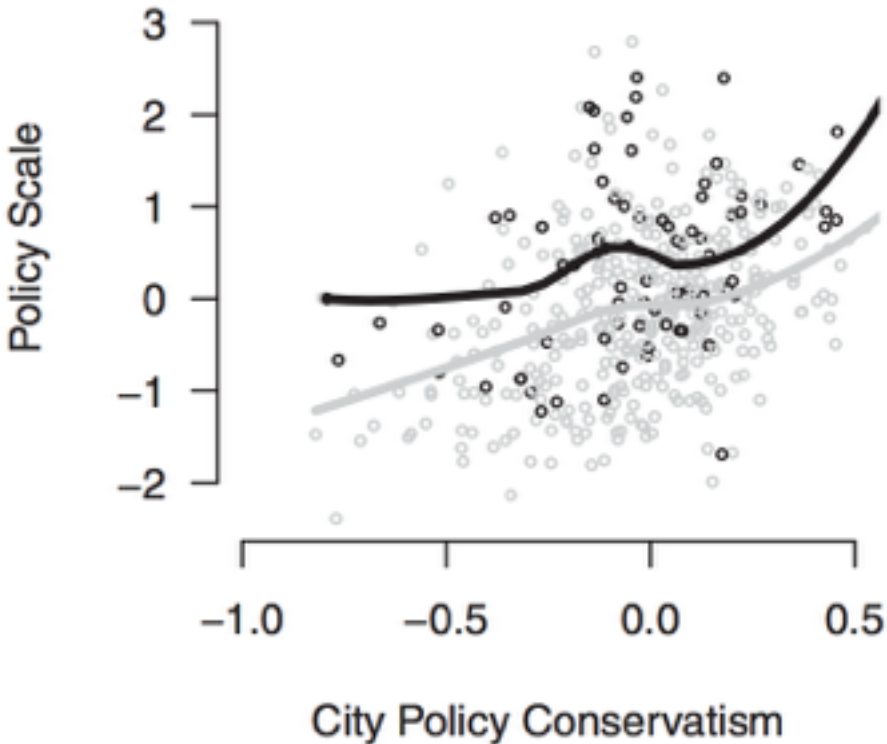
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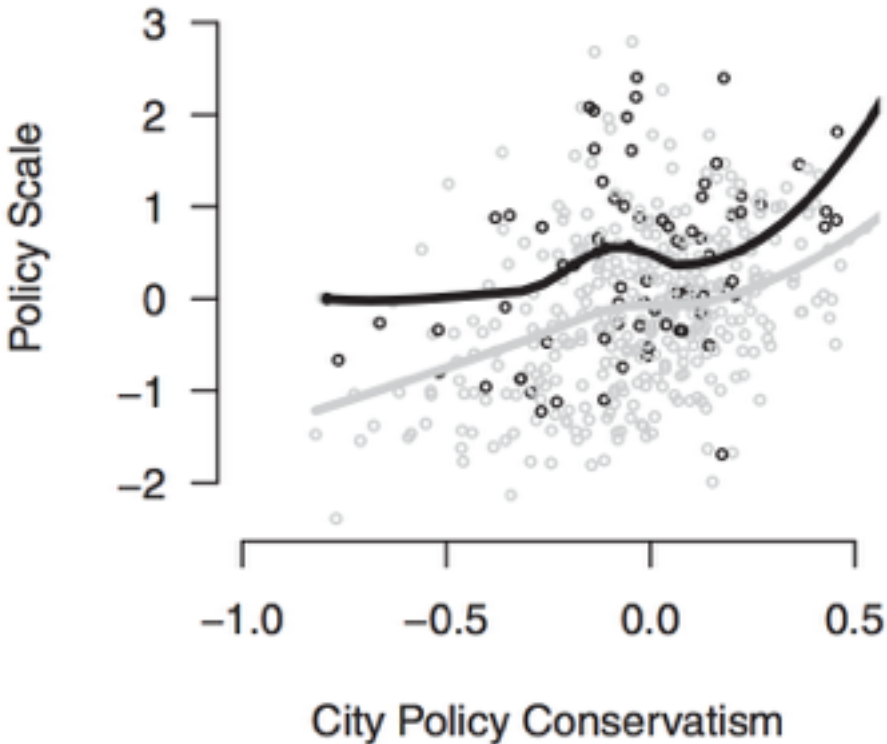


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- There are many ways to contribute. Choose some combination of:
 - better data
 - better design (e.g. causal inference)
 - better measurement
 - better theory

Often one of these makes possible another.